

Perfect valley filter in a topological domain wall

Hui Pan,¹ Xin Li,¹ Fan Zhang,^{2,*} and Shengyuan A. Yang^{3,†}

¹Department of Physics, Beihang University, Beijing 100191, China

²Department of Physics, University of Texas at Dallas, Richardson, Texas 75080, USA

³Research Laboratory for Quantum Materials, Singapore University of Technology and Design, Singapore 487372, Singapore

(Received 31 December 2014; revised manuscript received 31 March 2015; published 7 July 2015)

We propose a realization of perfect valley filters based on the chiral domain-wall channels between a quantum anomalous Hall insulator and a quantum valley Hall insulator. Uniquely, all these channels reside in the same valley and propagate unidirectionally, 100% valley-polarizing passing-by carriers without backscattering. The valley index, the chirality, and the number of the channels are protected by topological charges, controllable by external fields, and detectable by circular dichroism.

DOI: [10.1103/PhysRevB.92.041404](https://doi.org/10.1103/PhysRevB.92.041404)

PACS number(s): 73.43.Cd, 71.70.Ej, 73.22.-f, 73.63.-b

Many crystalline materials have two or more degenerate energy extrema in momentum space, which endows the low-energy carriers with a valley degree of freedom. Following the extensive studies in spintronics, there has been a growing interest in exploring the possibility of manipulating valley degrees for information processing, leading to a concept of valleytronics [1–8]. For practical valleytronics applications, it is critical to have a controllable and efficient way to generate the valley polarization of carriers. Although recent experiments have succeeded in generating and modulating the valley polarization dynamically by circularly polarized lights in monolayer transition metal dichalcogenides [9–12], it is yet desired to have valley control by static means in transport [13–15]. To this end, a valley filter is an indispensable component in valleytronics devices. Several schemes of valley filters have been suggested in the context of graphene, e.g., by using nanoconstriction [1], irradiation [16], line defects [17], strain engineering [18], or the recently proposed valley-polarized quantum anomalous Hall (QAH) phase [5,19,20]. Since in these filters the propagating modes of both valleys generally coexist, it is arduous to achieve perfect filtering due to intervalley scattering caused by lattice-scale defects, which are challenging to completely eliminate during fabrication.

Motivated by the spontaneous domain walls [21,22] that may exist in ultra-clean interacting bilayer graphene [23], here we propose a general scheme for creating a perfect valley filter in honeycomb-lattice materials utilizing a domain wall (DW) [21,22,24–31] between two topologically distinct insulating regions: a QAH insulator [5,32–35] breaking time-reversal symmetry (\mathcal{T}) and a quantum valley Hall (QVH) insulator [3,5] breaking inversion symmetry (\mathcal{P}). Since both symmetries are destroyed, the valley filtering becomes efficient. It turns out that subgap-propagating chiral channels appear in the DW, which are dictated by a change in the bulk topological charge across the DW [24,27,36]. Remarkably enough, all the unidirectional channels reside in the same valley when the valley-projected topological charge only changes at one designed valley across the DW. As a result, carriers in the filter could achieve 100% valley polarization without any backscattering. Due to its topological origin, the performance

of such a filter is robust against scattering and structural imperfections. We show that both the valley index and the chirality of our proposed elementary filter can be easily controlled by external fields and can be probed by optical circular dichroism, which allows versatile valleytronics functionalities achieved in a relatively simple design.

Toy model. We first present our basic idea through the analysis of a toy model. Consider a spinless fermion model defined on a two-dimensional (2D) honeycomb lattice [Fig. 1(a)],

$$\mathcal{H} = t \sum_{\langle i,j \rangle} c_i^\dagger c_j + it_2 \sum_{\langle\langle i,j \rangle\rangle} v_{ij} c_i^\dagger c_j + \lambda_v \sum_i \xi_i c_i^\dagger c_i. \quad (1)$$

Here the first term represents the nearest-neighbor hopping. The second term, first introduced by Haldane [32], connects the next-nearest neighbors, with $v_{ij} = +(-)$ if the electron makes a left (right) turn when hopping from site j to site i [37]. The last term is a staggered potential with opposite signs ($\xi_i = \pm 1$) on different sublattices [37]. In the absence of the last two terms in (1), it is known that near half filling the energy dispersion is gapless and linear down to the K and K' Dirac points, i.e., the two inequivalent corners of the hexagonal Brillouin zone. The two valleys are related by \mathcal{T} and \mathcal{P} symmetry operations. The gapless Dirac point at each valley is protected by a sublattice symmetry and the winding number of an infinitesimal Fermi circle. Both the Haldane term and the staggered potential open energy gaps at the Dirac points, as each breaks the sublattice symmetry. Importantly, the Haldane term breaks \mathcal{T} and the staggered potential breaks \mathcal{P} . We consider a DW formed by a spatial separation of the two topologically distinct states, e.g., t_2 (λ_v) to be nonzero only for region $y > 0$ ($y < 0$), as shown in Fig. 1(b). Figure 1(c) plots the energy spectrum with such a DW along the zigzag direction in order for the two valleys to be distinguished. In the bulk band gap, remarkably, there appears to be a chiral gapless channel attached to valley K , localized at the DW, and propagating along the $+\hat{x}$ direction.

To gain a better understanding of this chiral gapless valley-filtered channel, we focus on the low-energy physics of the toy model. Away from the DW, taking t as the largest energy scale, we expand the Hamiltonian around the K (K') point and obtain a continuum model $H_{\text{eff}} = H_0 + H_\Delta$, where the band term $H_0 = v_F(\tau_x k_x \sigma_x + k_y \sigma_y)$ and the mass term $H_\Delta = -\lambda_a \tau_z \sigma_z$ ($\lambda_a = 3\sqrt{3}t_2$) for $y \rightarrow +\infty$ and $\lambda_v \sigma_z$ for

*zhang@utdallas.edu

†shengyuan_yang@sutd.edu.sg

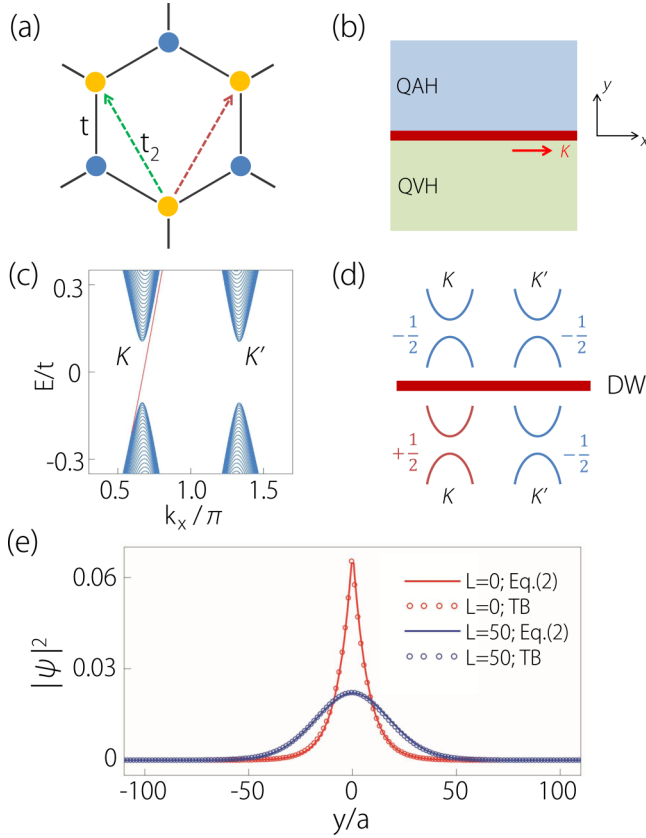


FIG. 1. (Color online) The realization of a perfect valley filter. (a) The lattice model described by Eq. (1). Blue and yellow dots denote the two sublattices. Representative next-nearest-neighbor hoppings are indicated by the red (green) arrows with $v_{ij} = +(-)$. (b) Schematics of the topological DW proposed in the main text. (c) The energy spectrum [38] of (b) with a valley-filtered chiral DW channel. (d) The valley-projected topological charges on the two sides of the DW. (e) Wave-function distribution for the zero energy mode at valley K . Here we take two different DW widths L (in units of a) for a DW with a $\tanh(y/L)$ profile for the mass term. The solid lines are from Eq. (2) and the circles are solutions from the tight-binding model.

$y \rightarrow -\infty$. Here the wave vector k is measured from the K (K') point, $v_F = 3at/2$ is the Fermi velocity with a the distance between nearest neighbors, $\tau_z = \pm$ denotes the two valleys, Pauli matrices σ act on the sublattice pseudospin, and we assume that $\lambda_v, \lambda_a, v_F > 0$. One observes that H_{eff} of valley K is a gapped two-band model with a mass sign reversal across the DW. It is quintessential that such a Jackiw-Rebbi problem [39] bears a zero mode,

$$\psi_{k_x}(\mathbf{r}) = \frac{1}{A} \begin{pmatrix} 1 \\ 1 \end{pmatrix} \exp \left[ik_x x + \frac{1}{v_F} \int_0^y \Delta(y') dy' \right], \quad (2)$$

where A is a normalization constant and the mass Δ is defined through $H_\Delta = \Delta(y)\sigma_z$. This mode is exponentially localized at the DW, with a chiral dispersion $E = v_F k_x$ around zero energy. In Fig. 1(e), we plot the wave-function distribution of the DW mode for a sharp DW and for a DW with finite width. Beneficially, the presence of such a chiral gapless DW channel depends only on the designed signs of Δ at $y = \pm\infty$,

regardless of the detailed DW characteristics, which reflect its topological nature.

The robustness of the chiral gapless DW channel is intimately connected to the change in the bulk topological charges across the DW [5,24,27,36]. Either side of the DW has a valley-projected topological charge $\mathcal{N} = \frac{1}{2\pi} \int d^2k \Omega(\mathbf{k})$ [24,26], where $\Omega(\mathbf{k}) \equiv \nabla_{\mathbf{k}} \times \mathcal{A}(\mathbf{k})$ and $\mathcal{A}(\mathbf{k}) \equiv \langle u_{\mathbf{k}} | i \nabla_{\mathbf{k}} | u_{\mathbf{k}} \rangle$ are the Berry curvature and the Berry connection of the valence bands, with $|u_{\mathbf{k}}\rangle$ being the periodic part of the Bloch eigenstate. The Berry curvature is out of plane for the 2D case and concentrated around each valley center in our model. For the continuum model H_{eff} , we obtain $\mathcal{N} = \tau_z \text{sgn}(\Delta)/2$. Since $\Delta = -\lambda_a \tau_z$ in the QAH domain ($y > 0$), $\mathcal{N} = -1/2$ for both valleys, where the valley independence is dictated by \mathcal{P} . Evidently, the total topological charge of both valleys (Chern number) is one, featuring a QAH state. In the QVH domain with $\Delta = \lambda_v$ ($y < 0$), $\mathcal{N} = \tau_z/2$, where the opposite topological charges of different valleys are a consequence of \mathcal{T} (in this sense the QVH state is analogous to the quantum spin Hall state [5,37]). These topological charges are illustrated in Fig. 1(d). The number of valley-dependent gapless chiral DW modes is related to the difference in topological charges across the DW by an index theorem [24,25,36]. More specifically, for each valley v , the number of chiral modes moving in the $+\hat{x}$ direction minus the number of chiral modes moving in the $-\hat{x}$ direction is equal to the difference of the bulk topological charges \mathcal{N} on the two sides of the DW, $\nu = \mathcal{N}(y < 0) - \mathcal{N}(y > 0)$. It follows that $\nu = 1$ for valley K and $\nu = 0$ for valley K' in our case. Consequently, one chiral gapless channel is protected at K whereas none is at K' . This topological argument is consistent with our previous analysis.

The above analysis demonstrates that when, across the DW, the valley-projected topological charge changes (by an integer) for only one valley, the DW is guaranteed to possess valley-filtered chiral modes. Because all the propagating channels in the bulk gap are of the same valley, scattering cannot change the carriers' valley index, and because of the chiral nature of these channels, there is no backscattering near the Fermi energy (assumed in the bulk gap). As a result, such a DW is perfectly transparent for one valley but completely opaque for the other valley, hence behaving as a perfect valley filter.

Regarding the valley filter's operation, the DW does not need to be exactly along the zigzag direction. It works as long as the two valleys can be distinguished when projected along the DW mode propagating direction. The DW profile may vary along the filter, because, based on the above topological argument, the presence of the DW channels is insensitive to the detailed wall profile (e.g., the orientation), and backscattering and intervalley scattering are suppressed due to the absence of corresponding scattering channels, analogous to the edge transport in the quantum Hall effect. Also, control of DW is through macroscopic external means (e.g., by gate voltages, as discussed below), which are smooth at the lattice scale. As long as the DW is smooth at the lattice scale, the intervalley scattering way below the Fermi level is also suppressed.

Field control of the valley filter. Now we examine a more realistic system where spin is included and demonstrate the versatile operating modes of the valley filter which can be controlled by external electric and magnetic fields. Consider a tight-binding model \mathcal{H}_0 of a honeycomb lattice with the usual

nearest-neighbor hopping, as the t term in Eq. (1). Again, the QVH domain can be realized by a \mathcal{P} -breaking staggered sublattice potential \mathcal{H}_v , as the λ_v term in Eq. (1). Physically, such a staggered potential can arise from an interaction with a substrate [40] or from the occupation of the two sublattices by different atoms or atomic orbitals [7,41]. Of particular interest is the case in which the two sublattices are slightly shifted out of plane with respect to each other, forming a buckled structure. Such buckling has been found in 2D materials such as silicene [42], germanene [42], and quite a few chemically functionalized materials [43–46]. In this class of materials \mathcal{H}_v can be induced and tuned by a perpendicular electric field.

Regarding the QAH domain, it can be engineered by a Rashba spin-orbit coupling $\mathcal{H}_R = it_R \sum_{(i,j),\alpha\beta} c_{i\alpha}^\dagger (s^{\alpha\beta} \times \mathbf{d}_{ij})_z c_{j\beta}$ combined with an exchange coupling $\mathcal{H}_M = M \sum_{i,\alpha\beta} c_{i\alpha}^\dagger s_z^{\alpha\beta} c_{i\beta}$, where \mathbf{d}_{ij} is a unit vector pointing from site j to site i and s are the spin Pauli matrices. The \mathcal{T} -breaking exchange coupling lifts the spin degeneracy producing a band inversion, whereas the \mathcal{P} -breaking Rashba term hybridizes the inverted bands yielding an energy gap. Such a QAH model has been well demonstrated in the context of graphene [33–35,47]. The Rashba and the exchange couplings can be produced simultaneously by ferromagnetic adsorbed atoms [33,48] or in proximity to a(n) (anti)ferromagnetic substrate [47,49].

A straightforward calculation yields that the valley-contrasting topological charge is $\tau_z \text{sgn}(\lambda_v)$ for the QVH state with $\mathcal{H}_{\text{QVH}} = \mathcal{H}_0 + \mathcal{H}_v$ and $\text{sgn}(M)$ for the QAH state with $\mathcal{H}_{\text{QAH}} = \mathcal{H}_0 + \mathcal{H}_R + \mathcal{H}_M$, respectively. Therefore, at a DW between the two states, the number of chiral gapless DW channels at valley τ_z must be

$$\nu = \tau_z \text{sgn}(\lambda_v) - \text{sgn}(M), \quad (3)$$

based on the bulk-boundary correspondence, as we discussed above. Again, the important consequence is that the chiral gapless DW channels must appear and only appear in a single valley. As an example, when $\lambda_v > 0$ and $M < 0$, $\nu = 2$ for valley K and $\nu = 0$ for valley K' . This implies there are two DW channels propagating in the $+\hat{x}$ direction at valley K and no state at valley K' , which is confirmed by our numerical calculation and is shown in Fig. 2(a). These DW states can also be solved in a low-energy continuum model, similar to what we have done for the toy model.

It follows from Eq. (3) that both the valley index of the DW channels and their propagating direction (chirality) are determined by the signs of λ_v and M , which may be manipulated by tuning the external electric and magnetic fields. In Fig. 2(b), we schematically show how the characteristics of the DW channels vary as the signs of λ_v and M are switched. The two axes ($\lambda_v = 0$ and $M = 0$) correspond to topological phase boundaries at which the bulk gap vanishes. Equation (3) and Fig. 2(b) are suggestive of a versatile control of the operating modes for the valley filter. As an example, consider an initial mode with $\lambda_v > 0$ and $M < 0$. By flipping only the sign of λ_v , the valley index becomes opposite whereas the chirality remains the same. By inverting the signs of both λ_v and M , the valley index is maintained whereas the chirality is reversed. Both the valley and chirality modes can be switched simultaneously by a sign reversal of M . All these

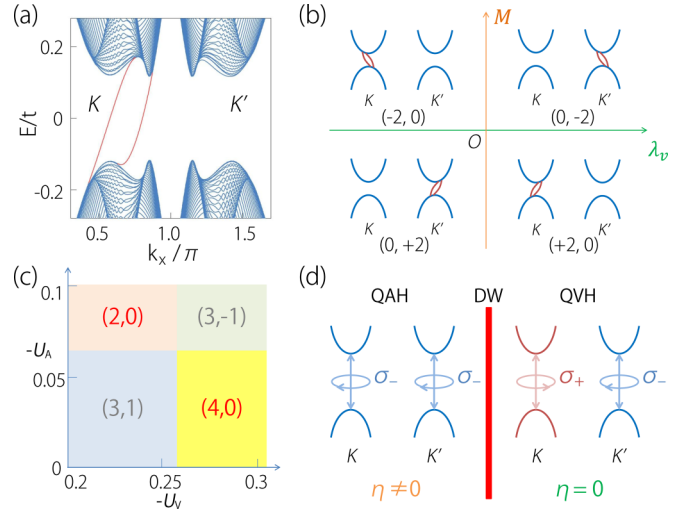


FIG. 2. (Color online) (a) Energy spectrum of the monolayer model featuring two valley-filtered chiral DW channels (in red) [50]. (b) $(\nu_K, \nu_{K'})$ as a function of the exchange coupling M and the sublattice staggered potential λ_v in the monolayer model. (c) $(\nu_K, \nu_{K'})$ in the bilayer model, tuned by the interlayer potential differences U_V and U_A on the two sides of the DW [50]. (d) Optical circular dichroism (with light frequency of the bulk gap) exhibiting contrasting features across the DW.

characteristics can also be easily argued from the symmetry point of view.

All of the above discussions can be directly extended to a bilayer system that may exhibit a richer topological phase diagram due to the additional layer degree of freedom. We consider an AB -stacked bilayer graphene model following Ref. [51]. Each layer is described by the same Hamiltonian $\mathcal{H}_0 + \mathcal{H}_R + \mathcal{H}_M$, as discussed above. The two layers are coupled by the interlayer hopping, $\mathcal{H}_t = t_\perp \sum_{(i \in (t,A), j \in (b,B))} c_i^\dagger c_j$, between the A site of the top layer and the B site of the bottom layer that are the nearest interlayer neighbors. Through dual gating, it is convenient to introduce an interlayer potential difference $\mathcal{H}_U = U \sum_i \zeta_i c_i^\dagger c_i$, with $\zeta_i = \pm$ denoting the top and bottom layers. \mathcal{H}_U plays a role here that is similar to that of the staggered sublattice potential \mathcal{H}_v in the buckled monolayer system. Depending on the competition between the exchange coupling \mathcal{H}_M and other potentials, various distinct QVH and QAH states can be realized [20,51,52].

Compared to the monolayer case, of particular interest in the bilayer case is that its valley-projected topological charge can have a magnitude of either one or two, depending on the model parameters [51]. As a consequence, at the DW between the bilayer QAH and QVH states, there exist two types of perfect valley filters with a different number of chiral DW channels: For one type it has two perfect valley-filtered channels, whereas for the other type it has four. In Fig. 2(c), we plot $(\nu_K, \nu_{K'})$, the number of chiral channels in each valley, as a function of U_A and U_V , with other parameters fixed. Here we have assumed that the interlayer potential differences on the two sides of the DW, denoted by U_A (U_V) for the QAH (QVH) domain, can be controlled independently. One notes that in the chosen parameter range, there are four regions of $(\nu_K, \nu_{K'})$, of which (2,0) and (4,0) are perfect valley filters, whereas the

other two have DW channels in both valleys. Nonetheless, this indicates that by controlling the interlayer potentials, it is possible to tune the conductance of a perfect valley filter, e.g., from $2e^2/h$ to $4e^2/h$ when the phase switches from (2,0) to (4,0).

Optical circular dichroism. Conventionally, gapless DW modes can be probed by transport or scanning tunneling spectroscopy. Since a perfect valley filter requires the breaking of \mathcal{T} , optical circular dichroism may also be employed to detect the presence, the location, and the characteristics of a topological DW bearing a perfect valley filter. We sketch the circular dichroism in Fig. 2(d) for our model and illustrate the physics below using the standard argument of Fermi's golden rule. The coupling strength of an interband optical transition with σ_{\pm} circularly polarized light is given by $\mathcal{M}_{\pm}(\mathbf{k}) = \mathcal{M}_x \pm i\mathcal{M}_y$, where $\mathcal{M}_{\mu} = \langle u_{\mathbf{k}}^c | \nabla_{\mathbf{k}_{\mu}} H | u_{\mathbf{k}}^v \rangle$ is the interband matrix element. For a valley-projected chiral two-band system [5] with a gap 2Δ , e.g., gapped monolayer or bilayer graphene, the absorbance [4,53] of the σ_{\pm} light with frequency ω has a universal form $\propto (1 \pm 2\tau_z \Delta / \omega)^2 \Theta(\omega - 2\Delta)$. When the optical frequency is close to the band gap, at valley K (K') the interband transition occurs only for σ_+ (σ_-) circular polarization. For the QVH state, the net circular dichroism $\eta = (|\mathcal{M}_+|^2 - |\mathcal{M}_-|^2) / (|\mathcal{M}_+|^2 + |\mathcal{M}_-|^2)$ vanishes, as required by \mathcal{T} . In contrast, for the QAH state breaking \mathcal{T} , there is a strong circular dichroism. Therefore, such a difference between the two domains in optical absorbance or photoluminescence can be used to probe the presence and the location of the valley filter. Since $|\mathcal{M}_{\pm}|^2$ also depends on the sign of Δ , the circular dichroism can also probe to the character of the valley filter that is sensitive to the sign of Δ .

Discussion. We have proposed a general scheme for creating perfect valley-filtered channels at the DW between two topologically distinct insulating regions. The ease of

local field control of each filter will allow the construction of more complex valleytronic devices using multiple DWs or a percolating DW network. For example, a valley valve can be constructed by combining two valley filters in a series. Whether a current can pass through the valve depends on whether the two filters have the same valley index and the same chirality, which can be controlled by local electric and/or magnetic fields.

Although it is not a focus here to investigate the specific material realization of our valley filter, we do note that it is promising to obtain the desired topological DWs in 2D materials with a hexagonal lattice symmetry, such as single or multilayer graphene, silicene, and chemically functionalized monolayer materials, for which the realizations of both the QVH and QAH states have been well studied. Notably, most recently, the QVH state appears to have been realized in a graphene experiment by breaking sublattice inversion symmetry via a h -BN substrate [15] and in a bilayer graphene experiment by breaking layer inversion symmetry via an electric field [54]. The QAH state in graphene, not yet realized though, has been extensively studied and two routes appear to be promising. One route is to deposit magnetic atoms [33,48] onto the honeycomb lattice and the other route is by proximity coupling the lattice to a(n) (anti)ferromagnetic substrate [47].

Our scheme can also be generalized to materials with more than two valleys [55], and a perfect valley filter can be created whenever, across a DW, the valley-projected topological charge only changes at one designed valley.

The authors thank D. L. Deng for helpful discussions. H.P. is supported by the NSFC under Grant No. 11174022 and the NCET program of MOE, F.Z. is supported by UT Dallas research enhancement funds, and S.A.Y. is supported by SUTD-SRG-EPD2013062.

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- [1] A. Rycerz, J. Tworzydło, and C. W. J. Beenakker, *Nat. Phys.* **3**, 172 (2007).
 - [2] O. Gunawan, Y. P. Shkolnikov, K. Vakili, T. Gokmen, E. P. De Poortere, and M. Shayegan, *Phys. Rev. Lett.* **97**, 186404 (2006).
 - [3] D. Xiao, W. Yao, and Q. Niu, *Phys. Rev. Lett.* **99**, 236809 (2007).
 - [4] W. Yao, D. Xiao, and Q. Niu, *Phys. Rev. B* **77**, 235406 (2008).
 - [5] F. Zhang, J. Jung, G. A. Fiete, Q. Niu, and A. H. MacDonald, *Phys. Rev. Lett.* **106**, 156801 (2011).
 - [6] Z. Zhu, A. Collaudin, B. Fauque, W. Kang, and K. Behnia, *Nat. Phys.* **8**, 89 (2012).
 - [7] D. Xiao, G.-B. Liu, W. Feng, X. Xu, and W. Yao, *Phys. Rev. Lett.* **108**, 196802 (2012).
 - [8] T. Cai, S. A. Yang, X. Li, F. Zhang, J. Shi, W. Yao, and Q. Niu, *Phys. Rev. B* **88**, 115140 (2013).
 - [9] H. Zeng, J. Dai, W. Yao, D. Xiao, and X. Cui, *Nat. Nanotechnol.* **7**, 490 (2012).
 - [10] K. F. Mak, K. He, J. Shan, and T. F. Heinz, *Nat. Nanotechnol.* **7**, 494 (2012).
 - [11] T. Cao, G. Wang, W. Han, H. Ye, C. Zhu, J. Shi, Q. Niu, P. Tan, E. Wang, B. Liu, and J. Feng, *Nat. Commun.* **3**, 887 (2012).
 - [12] X. Xu, W. Yao, D. Xiao, and T. F. Heinz, *Nat. Phys.* **10**, 343 (2014).
 - [13] B. W. H. Baugher, H. O. H. Churchill, Y. Yang, and P. Jarillo-Herrero, *Nat. Nanotechnol.* **9**, 262 (2014).
 - [14] K. F. Mak, K. L. McGill, J. Park, and P. L. McEuen, *Science* **344**, 1489 (2014).
 - [15] R. V. Gorbachev, J. C. W. Song, G. L. Yu, A. V. Kretinin, F. Withers, Y. Cao, A. Mishchenko, I. V. Grigorieva, K. S. Novoselov, L. S. Levitov, and A. K. Geim, *Science* **346**, 448 (2014).
 - [16] D. S. L. Abergel and T. Chakraborty, *Appl. Phys. Lett.* **95**, 062107 (2009).
 - [17] D. Gunlycke and C. T. White, *Phys. Rev. Lett.* **106**, 136806 (2011).
 - [18] Y. Jiang, T. Low, K. Chang, M. I. Katsnelson, and F. Guinea, *Phys. Rev. Lett.* **110**, 046601 (2013).
 - [19] H. Pan, Z. Li, C.-C. Liu, G. Zhu, Z. Qiao, and Y. Yao, *Phys. Rev. Lett.* **112**, 106802 (2014).
 - [20] H. Pan, X. Li, H. Jiang, Y. Yao, and S. A. Yang, *Phys. Rev. B* **91**, 045404 (2015).

- [21] F. Zhang, J. Jung, and A. H. MacDonald, *J. Phys. Conf. Ser.* **334**, 012002 (2011).
- [22] X. Li, F. Zhang, Q. Niu, and A. H. MacDonald, *Phys. Rev. Lett.* **113**, 116803 (2014).
- [23] W. Bao *et al.*, *Proc. Natl Acad. Sci. USA* **109**, 10802 (2012).
- [24] I. Martin, Y. M. Blanter, and A. F. Morpurgo, *Phys. Rev. Lett.* **100**, 036804 (2008).
- [25] G. W. Semenoff, V. Semenoff, and F. Zhou, *Phys. Rev. Lett.* **101**, 087204 (2008).
- [26] W. Yao, S. A. Yang, and Q. Niu, *Phys. Rev. Lett.* **102**, 096801 (2009).
- [27] F. Zhang, A. H. MacDonald, and E. J. Mele, *Proc. Natl. Acad. Sci. USA* **110**, 10546 (2013).
- [28] J. S. Alden, A. W. Tsen, P. Y. Huang, R. Hovden, L. Brown, J. Park, D. A. Muller, and P. L. McEuen, *Proc. Natl. Acad. Sci. USA* **110**, 11256 (2013).
- [29] A. Vaezi, Y. Liang, D. H. Ngai, L. Yang, and E. A. Kim, *Phys. Rev. X* **3**, 021018 (2013).
- [30] D. S. L. Abergel, J. M. Edge, and A. V. Balatsky, *New J. Phys.* **16**, 065012 (2014).
- [31] Y. Kim, K. Choi, J. Ihm, and H. Jin, *Phys. Rev. B* **89**, 085429 (2014).
- [32] F. D. M. Haldane, *Phys. Rev. Lett.* **61**, 2015 (1988).
- [33] Z. Qiao, S. A. Yang, W. Feng, W.-K. Tse, J. Ding, Y. Yao, J. Wang, and Q. Niu, *Phys. Rev. B* **82**, 161414(R) (2010).
- [34] W.-K. Tse, Z. Qiao, Y. Yao, A. H. MacDonald, and Q. Niu, *Phys. Rev. B* **83**, 155447 (2011).
- [35] Z. Qiao, H. Jiang, X. Li, Y. Yao, and Q. Niu, *Phys. Rev. B* **85**, 115439 (2012).
- [36] G. E. Volovik, *The Universe in a Helium Droplet* (Oxford University Press, New York, 2003).
- [37] C. L. Kane and E. J. Mele, *Phys. Rev. Lett.* **95**, 226801 (2005).
- [38] We have chosen $t_2 = 0.02$ (0) and $\lambda_v = 0$ (0.5) for the QAH (QVH) state.
- [39] R. Jackiw and C. Rebbi, *Phys. Rev. D* **13**, 3398 (1976).
- [40] S. Y. Zhou, G.-H. Gweon, A. V. Fedorov, P. N. First, W. A. de Heer, D.-H. Lee, F. Guinea, A. H. Castro Neto, and A. Lanzara, *Nat. Mater.* **6**, 770 (2007).
- [41] X. Li, F. Zhang, and Q. Niu, *Phys. Rev. Lett.* **110**, 066803 (2013).
- [42] S. Cahangirov, M. Topsakal, E. Akturk, H. Sahin, and S. Ciraci, *Phys. Rev. Lett.* **102**, 236804 (2009).
- [43] S.-H. Cheng, K. Zou, F. Okino, H. R. Gutierrez, A. Gupta, N. Shen, P. C. Eklund, J. O. Sofo, and J. Zhu, *Phys. Rev. B* **81**, 205435 (2010).
- [44] Y. Xu, B. Yan, H.-J. Zhang, J. Wang, G. Xu, P. Tang, W. Duan, and S.-C. Zhang, *Phys. Rev. Lett.* **111**, 136804 (2013).
- [45] C.-C. Liu, S. Guan, Z. Song, S. A. Yang, J. Yang, and Y. Yao, *Phys. Rev. B* **90**, 085431 (2014).
- [46] Z. Song, C.-C. Liu, J. Yang, J. Han, M. Ye, B. Fu, Y. Yang, Q. Niu, J. Lu, and Y. Yao, *NPG Asia Mater.* **6**, e147 (2014).
- [47] Z. Qiao, W. Ren, H. Chen, L. Bellaiche, Z. Zhang, A. H. MacDonald, and Q. Niu, *Phys. Rev. Lett.* **112**, 116404 (2014).
- [48] J. Ding, Z. Qiao, W. Feng, Y. Yao, and Q. Niu, *Phys. Rev. B* **84**, 195444 (2011).
- [49] J. Balakrishnan, G. K. W. Koon, M. Jaiswal, A. H. Castro Neto, and B. Özyilmaz, *Nat. Phys.* **9**, 284 (2013).
- [50] In Fig. 2(a), we have chosen $t_R = M = 0$ and $\lambda_v = 0.5$ for the QVH state, and $t_R = 0.1$, $M = -0.5$, and $\lambda_v = 0$ for the QAH state. In Fig. 2(c), we have chosen $t_R = 0.1$ and $M = 0$ for the QVH state, $t_R = 0.02$ and $M = -0.15$ for the QAH state, and $t_{\perp} = 0.15$ for both cases.
- [51] Z. Qiao, X. Li, W.-K. Tse, H. Jiang, Y. Yao, and Q. Niu, *Phys. Rev. B* **87**, 125405 (2013).
- [52] H. Pan, X. Li, Z. Qiao, C.-C. Liu, Y. Yao, and S. A. Yang, *New J. Phys.* **16**, 123015 (2014).
- [53] M. Trushin and J. Schliemann, *Phys. Rev. Lett.* **107**, 156801 (2011).
- [54] L. Ju *et al.*, *Nature (London)* **520**, 650 (2015).
- [55] Y. Shi, M. Wu, F. Zhang, and J. Feng, *Phys. Rev. B* **90**, 235114 (2014).



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Citation:

Pan, Hui, Xin Li, Fan Zhang, and Shengyuan A. Yang. 2015. "Perfect valley filter in a topological domain wall." *Physical Review B* 92(4), doi: 10.1103/PhysRevB.92.041404

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