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Near-Field MIMO-SAR Millimeter-Wave Imaging With Sparsely Sampled Aperture Data

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ABSTRACT
The primary challenge of a cost-effective and low-complexity near-field millimeter-wave (mmWave) imaging system is to achieve high resolution with a few antenna elements as possible. Multiple-input multiple-output (MIMO) radar using simultaneous operation of spatially diverse transmit and receive antennas is a good candidate to increase the number of available degrees of freedom. On the other hand, higher integration complexity of extremely dense transceiver electronics limits the use of MIMO only solutions within a relatively large imaging aperture. Hybrid concepts combining synthetic aperture radar (SAR) techniques and sparse MIMO arrays present a good compromise to achieve short data acquisition time and low complexity. However, compared with conventional monostatic sampling schemes, image reconstruction methods for MIMO-SAR are more complicated. In this paper, we propose a high-resolution mmWave imaging system combining 2-D MIMO arrays with SAR, along with a novel Fourier-based image reconstruction algorithm using sparsely sampled aperture data. The proposed algorithm is verified by both simulation and processing real data collected with our mmWave imager prototype utilizing commercially available 77-GHz MIMO radar sensors. The experimental results confirm that our complete solution presents a strong potential in high-resolution imaging with a significantly reduced number of antenna elements.

INDEX TERMS
Millimeter-wave radar (mmWave), near-field radar imaging, synthetic aperture radar (SAR), frequency-modulated continuous-wave (FMCW), multiple-input multiple-output (MIMO) radar, IWR1443 mmWave sensors.

I. INTRODUCTION
Millimeter-wave (mmWave) imaging technology has gained significant attention in recent years and it now plays an important role in many applications including medical diagnostics [1]–[3], security screening [4]–[9], and structure inspection [10]. The major challenges of building mmWave imaging systems are the cost and complexity arising from the need for a large number of transceiver elements.

The cross-range image resolution and the spatial sampling criteria are two key system parameters that determine the required number of antennas. While the range resolution is directly related to the bandwidth of the transmitting signal, the cross-range resolution is also determined by the effective length of the radar aperture. For example, an effective aperture size of 50 wavelengths (λ) along both horizontal and vertical directions is needed to achieve a 5 mm resolution in both axes at 50 cm range [4], [5]. On the other hand, λ/4 spacing is necessary between the measurement points to prevent the formation of unwanted imaging artifacts in a near-field scenario [4]. Hence, in order to satisfy the above mentioned image resolution under the required spatial sampling criteria, an ideal imaging system would consist of a two-dimensional (2-D) array with approximately 40000 antenna elements.

In recent years, great progress has been made in the semiconductor technology to enable cost-effective sensor solutions. Complementary metal-oxide semiconductor (CMOS) based frequency-modulated continuous-wave (FMCW) mmWave radars integrate all the analog and radio-frequency (RF) functionality as well as the low-level signal processing capability into a single chip with a compact form factor [11]. Such a highly integrated device enables the...
mmWave radar systems to be cost-effective and miniaturized. However, implementing densely placed transceivers required for high-resolution imaging is still a challenging effort.

A well-known approach to mitigate this challenge is the realization of multiple-input multiple-output (MIMO) array topologies [12]–[14]. Fully electronic multistatic sampling of large radar apertures using MIMO arrays has been incorporated into various near-field imaging systems [6], [15], [16]. While real-time operation is an ultimate goal for many applications, higher hardware complexity of integrating a large number of transceiver antennas makes fully electronic sampling less likely to be widely deployed. As a result, using a hybrid concept based on the combination of synthetic aperture radar (SAR) technique [17], [18] and MIMO array leads to lower hardware complexity than fully electronic sampling solutions [5], [19]. On the other hand, employing computationally efficient image reconstruction algorithms remains a challenge for MIMO-SAR configurations, especially in near-field imaging applications.

In near-field, the plane-wave assumption is invalid and the spherical electromagnetic wave model has to be used. The image reconstruction process must be able to completely compensate for the curvature of the wavefront. Although the time-domain correlation (or backprojection) method [5], [20], which provides a straightforward solution to estimate target area reflectivity by correlating the recorded data with the signature of a unit reflector at each spatial coordinate, can be used for any arbitrary multistatic array configuration, it suffers from high computational load.

For monostatic sampling schemes, where the measurements are taken by collocated transmit and receive antennas over regular spatial intervals, near-field image reconstruction has long been implemented using Fourier based inversion methods for both planar [4], [21], [22] and cylindrical/spherical [23], [24] scanning geometries. Unfortunately, these methods cannot be directly used for multistatic systems due to their need to consider the different trajectories of the incident and reflected electric fields.

Modified wavenumber domain image reconstruction algorithms accounting for multistatic array topology along with wavefront curvature in near-field have been presented for 2-D planar MIMO arrays [25], and for the systems synthesizing the 2-D aperture with one-dimensional (1-D) SAR along with 1-D MIMO sampling [19]. However, these techniques require uniform spatial sampling and involve computationally expensive wavenumber space interpolation. Hence, such needs limit the use of these algorithms for arbitrary array configurations and make them equally or less efficient than the direct time-domain reconstruction [5] in high throughput applications.

In response to all these major challenging requirements, we propose a novel near-field mmWave imaging solution that combines 2-D sparse MIMO arrays and SAR. We investigate the wavenumber domain of the backscattered data by expanding the study in [26] for SAR configuration. We establish the nonlinear relation between the wavenumber spectrum of the backscattered data and the reconstructed image, which, to our knowledge, has not been studied in the previous literature. We analyze the analytical effect of aliasing due to sparse sampling both on the wavenumber and spatial domains. We then propose an efficient Fourier based imaging algorithm for sparse MIMO-SAR to recover the spectrum of alias-free images by properly combining the overlapped spectrum of sparse subchannels.

The proposed image reconstruction algorithm for sparse multistatic sampling is based on the expansion of extremely efficient and interpolation-free Fourier based monostatic SAR imaging. To reconstruct near-field images from spatially diverse transmit and receive antennas, we introduce a multistatic-to-monostatic phase correction approach. In addition, the proposed reconstruction formula compensates the propagation loss, which is typically ignored in existing studies, to improve the imaging quality for the near-field operations.

To demonstrate the effect of sparse sampling and to validate the proposed image reconstruction algorithm, we build a mmWave imaging prototype utilizing commercially available MIMO sensors and a custom designed two-axis automatic rail system. We investigate key system parameters such as image resolution and spatial sampling criteria. We implement a calibration method to compensate the gain and phase mismatches of the MIMO array elements [27], [28]. We present real imaging results to show the effectiveness of proposed system that achieves high-resolution imaging performance with a significantly reduced number of antenna elements.

The rest of the paper is organized as follows. Section II presents the proposed MIMO-SAR configuration, and discusses the virtual antenna array concept in near-field using a multistatic-to-monostatic correction factor to improve Fourier based image formation. Section III reviews the standard monostatic SAR image reconstruction framework, which forms the basis of our MIMO-SAR image formation. Section IV addresses the signal processing steps involved in the proposed sparse MIMO-SAR image reconstruction starting with the wavenumber spectrum analysis of subsampling and its effect on the image domain, followed by the proposed novel image reconstruction technique that is compatible with the sparsely sampled aperture data. Section V discusses the image resolution, which is an important performance metric in imaging. Section VI presents the hardware architecture of the prototyped imager and MIMO array calibration. Simulations and measurement results are reported in Section VII, which is followed by conclusions.

II. SYSTEM MODEL

In this paper, we propose to synthesize a 2-D SAR aperture by mechanically scanning a MIMO array in a parallel track pattern as shown in Fig. 1. In the following subsections, we present the geometrical setup for the proposed MIMO-SAR system.
A. MIMO-SAR CONFIGURATION

The radar measurements are performed by moving a MIMO array continuously across the xy plane, along parallel lines, as shown in Fig. 1. Both SAR and MIMO apertures can be sparse. The unprimed and primed coordinates represent the measurement positions on the scan aperture and image pixel positions over a target aperture, respectively. In the established right-handed (x, y, z) Cartesian coordinate system, x-axis, y-axis, and z-axis denote horizontal, vertical, and depth directions, respectively.

The reference point (x, y, 0) is the position of the MIMO array at a specific measurement instant. The target aperture is at the distance of z₀. The image pixel coordinates are given as (x′, y′, z₀). In this paper, the target is assumed to be a 2-D object and parallel to the scanning plane. We will report our 3-D image formation results in a future article.

FIGURE 1. Geometry of SAR scanned in a parallel track pattern with a sparse MIMO array.

B. THE VIRTUAL ARRAY CONCEPT

We consider a sparse MIMO array equipped with M_T transmit and M_R receive antenna elements. Let the u-th transmit and the v-th receive antennas be located at r_u ∈ ℝ^3 and r_v ∈ ℝ^3, respectively, as shown in Fig. 2a. The transmit and receive antenna locations are characterized by

\[ g_T(r) = \sum_{u=0}^{M_T-1} \delta(r - r_u), \quad g_R(r) = \sum_{v=0}^{M_R-1} \delta(r - r_v). \] (1)

In a far-field scenario, assume that the distance to the target aperture is much larger than the distance between the transmit and receive elements of the MIMO array. This assumption leads to a conventional midpoint approximation that holds for a small fraction of \( \epsilon \) for each \( u \in \{1, \ldots, M_T\} \) and \( v \in \{1, \ldots, M_R\} \) as reported in [29],

\[ |r_u - r_v| \leq \sqrt{4\epsilon \lambda R}. \] (2)

where \( \lambda \) is the wavelength and \( R \) is the distance from the midpoint of the antennas to the ideal point scatterer. Then the corresponding transceiver antenna pair is approximated by a single monostatic virtual element located at [13], [29], [30]

\[ r_{uv} = (r_u + r_v)/2. \] (3)

The scaling factor of 1/2 is due to the round-trip propagation. The location of this monostatic virtual element as depicted in Fig. 2a is also called equivalent phase center. An example of MIMO array with \( M_T = 2 \) and \( M_R = 3 \) antennas and the corresponding virtual array are depicted in Fig. 2b. Thus, a MIMO array with \( M_T + M_R \) physical antennas can be approximated by a virtual array with \( L = M_T \times M_R \) monostatic elements. We can simplify the virtual element subscript as \( \ell \), where \( \ell \in \{1, \ldots, L\} \), for simplicity. Then the corresponding distribution function of the virtual array elements can be obtained by performing convolution of the transmitter and receiver element distributions in (1) as

\[ g_V(r) = g_T(r) \ast g_R(r) = \sum_{\ell=0}^{L-1} \delta(r - r_{\ell}). \] (4)

Therefore, the virtual array, which describes the set of independent monostatic elements that can collect the equivalent data, is half the size of the physical MIMO array (i.e., sum of the transmit and receive array aperture sizes) in each dimension. To create this virtual array architecture, receiver antennas must be able to separate the signals corresponding to different transmitter antennas. In this paper, the orthogonality between the transmit antennas is achieved by employing time division multiplexing (TDM) technique.

C. THE VIRTUAL ARRAY RESPONSE IN NEAR-FIELD IMAGING

For near-field imaging applications, small fraction of \( \epsilon \) assumption in (2) does not hold and an improved approximation is necessary. In the following, we will derive an efficient
proper adjustment factor to create an equivalent virtual array from a MIMO array for near-field scenarios.

Let us express the total round-trip distance associated with the $u$-th transmitter element at $(x_a, y_a, 0)$ and the $v$-th receiver element at $(x_r, y_r, 0)$ to a point scatterer at $(x', y', z_0)$ as

$$R_{tu} = R_u + R_v = \sqrt{(x_u - x')^2 + (y_u - y')^2 + z_0^2} + \sqrt{(x_v - x')^2 + (y_v - y')^2 + z_0^2}. \quad (5)$$

Let us denote the location of the virtual antenna element corresponding to the $u$-th transmitter and the $v$-th receiver as $(x, y)$. We can express the $u$-th transmitter and the $v$-th receiver locations as

$$x_u = x + d_{u}^x/2, \quad y_u = y + d_{u}^y/2,$$
$$x_v = x - d_{v}^x/2, \quad y_v = y - d_{v}^y/2, \quad (6)$$

where $d_{u}^x$ and $d_{v}^x$ are the distances between the transmitter and receiver elements in $x$ and $y$ axes, respectively, as shown in Fig. 2a. Applying multivariate Taylor series expansion to (5) up to third order terms with respect to the parameters $d_{u}^x$ and $d_{v}^x$ around zero, as described in the Appendix C, we can obtain

$$R_{tu} \approx 2R + \frac{(d_{u}^x)^2 + (d_{v}^x)^2}{4R} = \frac{(x - x')d_{u}^x + (y - y')d_{v}^x}{4R^3}. \quad (7)$$

where

$$R = \sqrt{(x - x')^2 + (y - y')^2 + z_0^2}. \quad (8)$$

is the distance between the midpoint and the scatterer. Considering $(x - x')$, $(y - y') \ll z_0$ for the second order terms in (7), we can obtain an improved approximation to the total round-trip distance associated with the $\ell$-th virtual element in terms of

$$R_{tu} \approx 2R + \frac{(d_{u}^x)^2 + (d_{v}^x)^2}{4z_0}. \quad (9)$$

**D. SIGNAL MODEL**

In recent years, several mmWave sensors based on FMCW signaling have been successfully constructed especially targeting automotive radar applications. FMCW (also known as chirp waveform) offers several advantages, i.e., large signal bandwidth, range processing gain, the inherent isolation between transmitters and receivers, and low sampling rate. Based on the improved virtual antenna array concept presented in the previous section and TDM technique, the transmit and receive antennas are paired to approximate a monostatic radar operation. Thus, let us briefly review a single element monostatic radar signal model.

Consider an FMCW signal transmitted by the monostatic antenna element in complex form as

$$m(t) = e^{j2\pi(f_0t+0.5K\tau^2)}, \quad 0 \leq t \leq T, \quad (10)$$

where $f_0$ is the carrier frequency at time $t = 0$, $K = B/T$ is the slope of frequency computed from the sweep bandwidth of $B$, and the chirp duration of $T$. Assuming an ideal point scatter at a distance of $R$, the received signal by the same monostatic antenna element is delayed and scaled version of the transmitted signal

$$s(t) = \sigma m(t - \tau) = \sigma e^{j2\pi(f_0(t-\tau)+0.5K\tau^2)}, \quad (11)$$

where $\tau = 2R/c$ is the round-trip delay of the echo for the target distance of $R$, $c$ is the speed of light, and $\sigma$ is the combination of target reflectivity and round-trip amplitude decay with range [25], [31]

$$\sigma = p/R^2, \quad (12)$$

where $p$ is the complex reflectivity of the ideal point target. The radar demodulates the received signal by mixing it with a copy of the transmitted signal to reduce the required system sampling rate. This is known as dechirping and results in a complex intermediate frequency (or beat) signal [32]

$$s(t) = \sigma e^{2\pi(f_0t+K\tau t-0.5K\tau^2)}, \quad (13)$$

where $K\tau$ term is the beat frequency which carries the range information. The last term of (13) is known as the residual video phase (RVP), which is found to be negligible [33]. Therefore, the beat signal can be rewritten in the wavenumber domain as

$$s(k) = p\frac{e^{j2kr}}{R^2}, \quad 2\pi f_0R/c \leq k \leq 2\pi f/c. \quad (14)$$

where $f_r = f_0 + KT$ is the maximum switch frequency of FMCW radar and $k = 2\pi f/c$ is the wavenumber corresponding to the frequency $f$.

Now we are ready to introduce the midpoint approximation derived in Section II-C. The approximation in (9) allows a MIMO array with sparsely placed transmit and receive elements to be converted to a virtual monostatic array more accurately for near-field imaging applications. The effectiveness of the image reconstruction is mainly determined by proper handling of the phase in (14), and any improvement in the amplitude decay with range will have little impact on the reconstructed image. Therefore, substituting (9) into the phase term in (14), we can express the received signal by the $\ell$-th hypothetical monostatic virtual element as

$$s_k(k) \approx p\frac{e^{j2Kr}}{R^2} = s(k)e^{j\phi_k(k)}, \quad (15)$$

where $s(k)$ is the signal that would be received by a physical monostatic element located at the same midpoint between actual transmitter and receiver antennas, and

$$\phi_k(k) = k\frac{(d_{u}^x)^2 + (d_{v}^x)^2}{4z_0}, \quad (16)$$

is the nonlinear phase term as a result of the improved approximation in (9) needed for near-field applications.

In the MIMO-SAR imaging configuration, the acquired 3-D backsattered data cube $s_k(x, y, z)$ from the $\ell$-th virtual channel is a function of two spatial coordinates, antenna pair spacing, target distance and the wavenumber. If the 2-D distributed target at $z_0$ is characterized by its complex reflectivity function $p(x', y')$, the main purpose of the
MIMO-SAR imaging algorithm is to recover \( p(x', y') \) from the reflected signals \( s_\ell(x, y, k) \) captured by all independent and arbitrary located virtual elements.

### III. IMAGE RECONSTRUCTION WITH MONOSTATIC SAR

Here, we review the standard monostatic SAR image reconstruction framework [4], [21], which forms the basis of our proposed algorithms. We adopt the signal model that assumes continuously recorded aperture data. Based on this model, we will determine the important relationship between \( k \)-domain (or spectral domain) and image domain (or spatial domain) when the imaging aperture is sparsely sampled by MIMO-SAR in Fig. 1.

We assume the linearized scattering model with the target reflectivity of \( p(x', y') \). By expanding the signal model in (14), we can express the received backscattered data from a planar target at a distance of \( z_0 \) as

\[
s(x, y, k) = \iiint p(x', y') \frac{e^{ikR}}{R} \, dx' \, dy',
\]

(17)

where \( R \) is the distance between the transceiver element and a general point on the target given in (8). We include the amplitude factor in the signal model due varying distance of MIMO array to the target. The amplitude factor (i.e., path loss) is typically ignored in the existing derivations. The target points are located at an average distance of \( z_0 \) from the aperture plane. Therefore, \( R^{-2} \) in (17) can be approximated by \( (z_0R)^{-1} \). The error introduced by this approximation will be negligible in the near-field applications [34]. \( z_0 \) is constant for a stationary object and, therefore, it can be ignored. As a result, the 2-D image reconstruction will be effectively approximated by a combination of the phase terms and the retained \( R^{-1} \) dependence that yields

\[
s(x, y, k) = \iiint p(x', y') \frac{e^{ikR}}{R} \, dx' \, dy'.
\]

(18)

Our derivation builds on the spirit of Weyl’s idea [35] of the representation of a spherical wave as a superposition of plane waves [36]

\[
\frac{e^{ikR}}{R} = \frac{j}{2\pi} \iiint \frac{e^{ik_\ell(x-x') + ik_y(y-y') + ik_z(z-z')}}{k_z} \, dk_x \, dk_y,
\]

(19)

where

\[
k_z = \sqrt{4k^2 - k_x^2 - k_y^2}.
\]

(20)

It is important to note that the plane waves are homogeneous when \( k_x^2 + k_y^2 \leq 4k^2 \), but they are inhomogeneous (significant only close to the plane \( z = 0 \)) otherwise. The entire derivation of (19) is given in the Appendix B.

After substituting (19) into (18), the backscattered data becomes

\[
s(x, y, k) = \frac{j}{2\pi} \iiint \iiint p(x', y') \frac{1}{k_z} \, e^{ik_\ell(x-x') + ik_y(y-y') + ik_z(z-z')} \, dk_x \, dk_y \, dx' \, dy'.
\]

(21)

Rearranging the order of integrals and using the 2-D Fourier transform definitions in the Appendix A gives

\[
s(x, y, k) = \frac{j}{2\pi} \iiint \iiint p(x', y') e^{-jk(x'+k_y'y')} \, dx' \, dy' \frac{\text{IFT}_{2D}[p(x, y)]}{k_z} = P(k_x, k_y).
\]

(22)

The distinction between the primed and unprimed coordinate systems above is dropped in the forward Fourier transform operation (denoted as \( \text{IFT}_{2D} \)) because they coincide. The outer double integral above represents a 2-D inverse Fourier transform over the \( xy \) domain. Hence, after dropping the constant terms, (22) becomes

\[
s(x, y, k) = \text{IFT}_{2D}[P(k_x, k_y)] = P(k_x, k_y).
\]

(23)

That yields

\[
P(k_x, k_y) = S(k_x, k_y)k_z e^{-jkz_0}.
\]

(24)

In (23), \( \text{IFT}_{2D} \) denotes 2-D inverse Fourier transform operation over the \( xy \) domain. (24) is then evaluated at multiple wavenumbers and coherently summed within an image plane [16] to reconstruct the 2-D target reflectivity as

\[
p(x, y) = \int \text{IFT}_{2D}[S(k_x, k_y)k_z e^{-jkz_0}] \, dk.
\]

(25)

Therefore, a monochromatic approach is assumed in the rest of the paper and \( k \) variable in the backscattered data is dropped for simplicity.

### IV. DEVELOPMENT OF IMAGE RECONSTRUCTION WITH SPARSE MIMO-SAR

The mmWave imager proposed and prototyped in this paper exploits sparse MIMO array configurations to reduce the cost and scanning time while providing high-resolution imaging. To recover images without any reconstruction artifacts, we investigate the response of the sparsely sampled MIMO-SAR imaging system to the target being imaged by establishing properties between spectral and spatial domains. As a first step, we review the analysis of the 1-D \( k \)-domain spectrum in terms of the dimensions of the target and the continuous finite SAR aperture. This analysis will enable us to develop a novel Fourier based imaging formulation compatible with sparsely sampled MIMO-SAR data.

#### A. WAVENUMBER SPECTRUM ANALYSIS AND SAMPLING CRITERION

Consider an imaging scenario, where the target area is centered with respect to the scanning system, as depicted in Fig. 3. While the analysis of the wavenumber spectrum here is limited to \( x \)-axis, the expressions can be easily expanded to \( y \)-axis. This approach is based on a prior knowledge of the total size of the target region under consideration instead of an unknown physical target geometry.
Denote $\theta_x$ as the limit of the system operating angle in $x-$axis, which is the lesser of the full beamwidth of the antenna or the angle covered by the aperture over the corresponding axis. Assuming the angle subtended by the aperture is less than the beamwidth of the antenna, we can express

$$\sin \theta_x = \frac{(D_S^x + D_T^x)/2}{(D_S^x + D_T^x)^2/4 + z_0^2},$$

(26)

where $D_S^x$ and $D_T^x$ are the SAR and target aperture sizes, respectively, as depicted in Fig. 1. As a result, the spectrum of the backscattered signal along $x-$axis will be limited to the region $[-k_{bw}^x, k_{bw}^x]$ where $k_{bw}^x$ is the highest wavenumber component defined as

$$k_{bw}^x \approx 2k \sin \theta_x.$$

(27)

Substituting (26) into (27) yields the bandwidth of the backscattered data collected along $x-$axis as

$$k_{bw}^x \approx \frac{2\pi(D_S^x + D_T^x)}{\lambda \sqrt{(D_S^x + D_T^x)^2/4 + z_0^2}}.$$

(28)

In MIMO-SAR imaging configuration, the backscattered signals are spatially sampled by transmit/receive antenna locations. While the proposed system employs sparse sampling, its development will be facilitated by understanding of the spatial sampling requirements based on monostatic scenario. As in the traditional time domain signals, sampling needs to satisfy the Nyquist criterion to avoid aliasing, but in space. The maximum theoretical limit of monostatic sampling of infinite aperture is $\lambda/4$ where $\lambda$ is the wavelength [4]. However, the spectrum of the backscattered data captured over a finite SAR aperture is limited by its size, spatial extent of the target aperture, and the distance between both apertures.

Consider a continuous spatial domain signal $s(x)$ captured in an imaging scheme in Fig. 3 and its Fourier transform (i.e., its wavenumber spectrum) $S(k_x)$. As expressed in (28), $S(k_x)$ is band-limited to $|k_x| \leq k_{bw}^x$. The corresponding minimum sampling wavenumber (i.e., the Nyquist rate) along $x-$axis is given by

$$k_{x}^s \geq 2k_{bw}^x = \frac{4\pi(D_S^x + D_T^x)}{\lambda \sqrt{(D_S^x + D_T^x)^2/4 + z_0^2}}.$$

(29)

Hence, $s(x)$ can be perfectly reconstructed from its samples without aliasing as long as the spatial sampling interval is [5]

$$\Delta_x \leq \Delta_x^{Nyq} = \frac{\pi}{k_{bw}^x} = \frac{\lambda \sqrt{(D_S^x + D_T^x)^2/4 + z_0^2}}{2(D_S^x + D_T^x)}.$$

(30)

**FIGURE 3.** Spectral domain of the backscattered data in $x-$axis.

**FIGURE 4.** Illustration of periodically nonuniform sampling of the continuous two-dimensional SAR aperture.

**B. ANALYSIS OF SPARSELY SAMPLED CONTINUOUS SAR APERTURE DATA**

MIMO array configurations can be used to reduce the hardware cost, software complexity, and data acquisition time. Our imaging setup is based on a sparse MIMO array, which is scanned mechanically in a plane as shown in Fig. 1. The radar waveforms transmitted by the MIMO array sample the continuous $xy$ plane as illustrated in Fig. 4. Based on the conversion of the MIMO array to the monostatic operation in (4) and the phase correction factor in (15), we can express spatially sampled version of the continuous SAR aperture data by the $\ell$th virtual channel as

$$s_\ell(x, y) = s(x, y)e^{j\phi_\ell} \times \sum_{p \in \mathbb{Z}} \sum_{q \in \mathbb{Z}} \delta(x - p\Delta_x - x_\ell, y - q\Delta_y - y_\ell),$$

(31)

where $\Delta_x$ and $\Delta_y$ are the sampling distances along $x$ and $y$ dimensions, respectively, as shown in Fig. 1. $s(x, y)$ above represents the backscattered data that would be received by a physical monostatic element over the continuous $xy$ aperture. $x_\ell$ and $y_\ell$ are the virtual element midpoint offsets in $x$ and $y$ axes, respectively, as depicted in Fig. 4.
Using the Fourier transform definitions in Appendix A, we can express the 2-D wavenumber spectrum of the sampled signal associated with the \( \ell \)th channel as

\[
S_\ell(k_x, k_y) = \frac{e^{j\phi_\ell}}{\Delta_x \Delta_y} \times \sum_{m \in \mathbb{Z}} \sum_{n \in \mathbb{Z}} S(k_x - mk_s^x, k_y - nk_s^y) \\
\times e^{-j(\ell mk_s^x + \ell nk_s^y)},
\]

subject to

\[
(k_x - mk_s^x)^2 + (k_y - nk_s^y)^2 \leq 4k^2,
\]

where

\[
k_s^x = \frac{2\pi}{\Delta_x}, \quad k_s^y = \frac{2\pi}{\Delta_y},
\]

are the spatial sampling frequencies.

C. EFFECT OF ALIASING ON THE IMAGE DOMAIN

Fourier transform properties are powerful tools for analyzing linear time invariant (LTI) systems. On the other hand, the relation between the wavenumber spectrum of the sub-sampled backscattered data and the reconstructed image is inherently nonlinear. To our knowledge, there is no prior work on establishing this nonlinear relation. Here, starting with the analysis in Section IV-B, we derive the analytical response of the reconstructed image to the aliasing components in the subsampled data spectrum.

Recall that the aliasing spectral component with index \( m \) and \( n \) (for \( \{m, n\} \neq \{0, 0\} \)) of the \( \ell \)th subchannel is defined in (32) as

\[
S_{mn}^\ell(k_x, k_y) = \frac{e^{j(\phi_\ell - (\ell mk_s^x + \ell nk_s^y))}}{\Delta_x \Delta_y} S(\hat{k}_x, \hat{k}_y),
\]

where

\[
\hat{k}_x = k_x - mk_s^x, \quad \hat{k}_y = k_y - nk_s^y.
\]

Using the relation between the backscattered data and the image spectra in (24), (36) becomes

\[
S_{mn}^\ell(k_x, k_y) = C_{mn}^\ell P(\hat{k}_x, \hat{k}_y) e^{i\hat{k}_z z_0}/\hat{k}_z, \quad (38)
\]

where

\[
\hat{k}_z = \sqrt{4k^2 - (\hat{k}_x)^2 - (\hat{k}_y)^2}.
\]

Substituting (38) into (24) yields the wavenumber spectrum of the imaging artifact (i.e., ghost image) created by the aliasing component as

\[
P_{mn}^\ell(k_x, k_y) = S_{mn}^\ell(k_x, k_y)\hat{k}_z e^{-i\hat{k}_z z_0} = C_{mn}^\ell P(\hat{k}_x, \hat{k}_y)\hat{k}_z e^{i\hat{k}_z z_0}. \quad (40)
\]

From (20) and (39), let us define the amplitude and the phase terms in (40) as

\[
\vartheta(k_x, k_y) = \frac{k_z}{\hat{k}_z} = \frac{\sqrt{4k^2 - k_x^2 - k_y^2}}{\sqrt{4k^2 - k_x^2 - k_y^2}}, \quad (41)
\]

and

\[
\varphi(k_x, k_y) = (\hat{k}_z - k_z)z_0 = \left(\sqrt{4k^2 - \hat{k}_x^2 - \hat{k}_y^2} - \sqrt{4k^2 - k_x^2 - k_y^2}\right)z_0. \quad (42)
\]

Applying first-order multivariate Taylor series expansion to (41) and (42) with respect to the parameters \( (k_x, k_y) \) around \( (mk_s^x, nk_s^y) \), as described in the Appendix C, the linear approximations of the amplitude and the phase terms become

\[
\vartheta(k_x, k_y) \approx \frac{2k}{G_{mn}} - \frac{mk_s^x}{2kG_{mn}} k_x - \frac{nk_s^y}{2kG_{mn}} k_y,
\]

\[
\varphi(k_x, k_y) \approx \frac{\hat{x}_{mn}}{G_{mn}} - \frac{mk_s^x}{2kG_{mn}} k_x - \frac{nk_s^y}{2kG_{mn}} k_y.
\]
\[ \varphi(k_x, k_y) \approx \frac{2k_0}{G_{mn}} \left( 1 - \frac{2k_x}{G_{mn}} \right) + \frac{mk_x^2 20}{G_{mn}} k_x + \frac{n k_y^2 20}{G_{mn}} k_y, \]

where

\[ G_{mn} = \sqrt{4k^2 - (mk_x^y)^2 - (nk_x^y)^2}. \]

Substituting (43) into (40), the wavenumber spectrum of the ghost image is approximated as

\[ P_{mn}^\ell(k_x, k_y) \approx C_{mn}^\ell P(\hat{k}^x, \hat{k}^y) e^{i\varphi_{mn}} \times (\theta_{mn} - \hat{x}_{mn} k_x - \hat{y}_{mn} k_y) \times e^{i(k_x x_{mn} + k_y y_{mn})}. \]

Using (37) and (45), let us define

\[ Q_{mn}^\ell(k_x, k_y) = (\alpha_{mn}^\ell - \beta_{mn}^\ell k_x - \gamma_{mn}^\ell k_y) \times P(k_x - mk_x^\ell, k_y - nk_y^\ell), \]

where

\[ \alpha_{mn}^\ell = \theta_{mn} C_{mn}^\ell e^{i\varphi_{mn}}, \]
\[ \beta_{mn}^\ell = \hat{x}_{mn} C_{mn}^\ell e^{i\varphi_{mn}}, \]
\[ \gamma_{mn}^\ell = \hat{y}_{mn} C_{mn}^\ell e^{i\varphi_{mn}}. \]

Substituting (46) into (45) yields

\[ P_{mn}^\ell(k_x, k_y) \approx Q_{mn}^\ell(k_x, k_y) e^{i(k_x x_{mn} + k_y y_{mn})}. \]

Using the Fourier transform definitions in the Appendix A, the ghost image created by the aliasing component is calculated as

\[ p_{mn}(x, y) \approx q_{mn}(x + x_{mn}, y + y_{mn}), \]

where (from (46))

\[ q_{mn}^\ell(x, y) = \text{IFT2D}\left[ Q_{mn}^\ell(k_x, k_y) \right] = \alpha_{mn}^\ell e^{i(mk_x^\ell x + nk_y^\ell y)} p(x, y) + j \beta_{mn}^\ell e^{i(mk_x^\ell x + nk_y^\ell y)} \frac{\partial}{\partial x} p(x, y) + j \gamma_{mn}^\ell e^{i(mk_x^\ell x + nk_y^\ell y)} \frac{\partial}{\partial y} p(x, y). \]

Hence, from (49) and (50), the ghost image created by an aliasing component in the subsampled wavenumber spectrum is the nonlinear operated alias-free image shifted by

\[ x_{mn} = \frac{mk_x^2 20}{G_{mn}}, \quad y_{mn} = \frac{n k_y^2 20}{G_{mn}}. \]

### D. IMAGE RECONSTRUCTION WITH SPARSELY SAMPLED MIMO-SAR DATA

As given in Section IV-B, if the spatial sampling intervals \( \Delta_x \) and \( \Delta_y \) do not meet the Nyquist criterion, aliasing that creates artifacts (i.e., ghosts) in the reconstructed image will occur as detailed in Section IV-C. Here, we propose a method for a sparse MIMO-SAR configuration to perfectly reconstruct alias-free images based on a multichannel combining technique using properly chosen complex gains. In other words, we show that the aliasing components in (36), which creates ghost images in (49), can be canceled by properly choosing a complex gain vector

\[ \mathbf{w} = [w_0 \ w_1 \ \ldots \ w_{L-1}]^T, \]

for \( L \) virtual channels, where \( (\cdot)^T \) denotes the transpose operation. The flow diagram of the MIMO-SAR sampling (as given in (31)) and the proposed image reconstruction scheme is depicted in Fig. 6.

Recall that the image reconstruction filter \( h(x, y) \) in Fig. 6 is given in (24) as

\[ h(x, y) = \text{IFT2D}\left[ k_c e^{-jk_x 20} \right], \]

where \( k_c \) is given in (20) and \( \text{IFT2D} \) denotes 2-D inverse Fourier transform operation over the \( xy \) domain. Combination of \( L \) subchannel spectrum in (32) using the complex gain vector in (52) is expressed as

\[ \mathbf{\tilde{s}}(k_x, k_y) = \sum_{\ell=0}^{L-1} \alpha_{mn}^\ell \tilde{s}(k_x - mk_x^\ell, k_y - nk_y^\ell) e^{-j(mk_x^\ell x + nk_y^\ell y)}. \]

In Section IV-B, we analyze the number of shifted copies in the wavenumber spectrum that must be canceled to reconstruct alias-free images of the targets with unknown sizes and proximity. Therefore, (35) yields the total number copies within the entire visible region. However, for a finite SAR aperture configuration with a prior knowledge of the target (see Section IV-A), the total number of aliasing terms in (54) that has to be canceled is limited by the indexes \( m \) and \( n \) as

\[ |mk_x^\ell| \leq 2k_{bw}^x, \quad |nk_y^\ell| \leq 2k_{bw}^y, \]

where \( k_{bw}^x \) and \( k_{bw}^y \) are the highest wavenumber components in \( x \) and \( y \) axes, respectively, as detailed in Section IV-A. Using the following vector notation

\[ \mathbf{\alpha}_{m,n} = [mk_x^\ell \ nk_y^\ell], \quad \mathbf{\beta}_\ell = [x_\ell \ y_\ell]^T, \]

![FIGURE 6. Reconstruction of image using sparsely sampled backscattered data by \( L \) virtual channels.](image)
we can rearrange (54) as
\[
\tilde{S}(k_x, k_y) = \frac{1}{\Delta_x \Delta_y} \left[ \left( \sum_{\ell=0}^{L-1} w_{\ell} e^{j\phi_{\ell}} \right) S(k_x, k_y) \right. \\
+ \left( \sum_{\ell=0}^{L-1} w_{\ell} e^{j(\phi_{\ell} - \alpha_1 \beta_{\ell})} \right) S(k_x, k_y - k_y^*) \\
+ \left( \sum_{\ell=0}^{L-1} w_{\ell} e^{j(\phi_{\ell} - \alpha_2 \beta_{\ell})} \right) S(k_x, k_y - 2k_y^*) + \ldots \\
\left. + \left( \sum_{\ell=0}^{L-1} w_{\ell} e^{j(\phi_{\ell} - \alpha_1,0 \beta_{\ell})} \right) S(k_x - k_x^*, k_y) + \ldots \right]. 
\]
\[(57)\]

Therefore, if the equation below has a solution for \(w\), all the aliasing terms are canceled to obtain alias-free backscattered data wavenumber spectrum \(S(k_x, k_y)\) in (57)
\[
\begin{bmatrix}
e^{j\phi_0} \\
e^{j(\phi_0 - \alpha_0 \beta_{0})} \\
\vdots \\
e^{j(\phi_{\ell} - \alpha_1,0 \beta_{\ell})} \\
\end{bmatrix}
\times
\begin{bmatrix}
w_0 \\
w_1 \\
\vdots \\
w_{L-1} \\
\end{bmatrix}
= 
\Delta_x \Delta_y \begin{bmatrix} 1 \\
0 \\
\vdots \\
0 \end{bmatrix}.
\]
\[(58)\]

Hence, expanding the reconstruction formula in (25), the solution for the gain vector in (58)
\[
w = (A^H A)^{-1} A^H e, \]
\[(59)\]
finally yields the 2-D monochromatic image reconstruction for MIMO-SAR as
\[
p(x, y) = \text{IFT}_{2D}[w^T S(k_x, k_y) k_x e^{-j\beta_{y0}}], \]
\[(60)\]
where
\[
S(k_x, k_y) = \begin{bmatrix} S_0(k_x, k_y) & \ldots & S_{L-1}(k_x, k_y) \end{bmatrix}^T, \]
\[(61)\]
is constructed by the wavenumber spectrum of the backscattered data sampled by \(L\) virtual channels. In (59), \((\cdot)^{-1}\) denotes the inverse and \((\cdot)^H\) denotes the conjugate transpose of a matrix. Using the same approach in (25), (60) is then evaluated at multiple wavenumbers and coherently summed within the image plane. As detailed in Section IV-B, each subchannel data \(s_{\ell}(x, y)\) is uniformly sampled over the \(xy\) domain. Therefore, the 2-D fast Fourier transform (FFT) may be used to obtain a sampled version of \(S_{\ell}(k_x, k_y)\). Assuming a discretization of \(N_x \times N_y\) points in the continuous \(xy\) plane with \(N_k\) sample points in the wavenumber domain, the computational complexity of the image reconstruction, which is dominated by the 2-D FFT operations in (61), can be approximated as \(L N_x N_y N_k \left(\log(N_x) + \log(N_y)\right)\).

It is important to note that, using the complex gains in (59), \(L - 1\) aliasing terms can be canceled using \(L\) subchannels. The proposed imaging method makes no assumption on the positions of the transmitters and receivers as long as the antenna layout and the sampling scenario ensure a well-conditioned \(A\) matrix in (58). Therefore, the proposed algorithm can be used for MIMO-SAR configurations using arbitrarily distributed transmit and receive antennas.

V. IMAGE RESOLUTION

The theoretical limit of the spatial resolution achieved in the reconstructed image is determined by width of the coverage in the wavenumber spectrum domain. In one dimension, a spectral coverage of width \(\Delta k\) results in a spatial pulselwidth of \(2\pi/\Delta k\) [4]. The spatial frequency width of the backscattered data in \(k_z\)-axis is \(2(k_T - k_0)\), where \(k_0\) and \(k_T\) are the wavenumbers correspond to the lowest and highest operating frequencies of the system \((f_0\) and \(f_T\), respectively, in (14)). Therefore, the depth (\(z\)-axis) resolution is determined by the bandwidth as
\[
\delta_z \approx \frac{2\pi}{2(k_T - k_0)} = \frac{c}{2(f_T - f_0)} = \frac{c}{2B}. \]
\[(62)\]

Similarly, from Section IV-A, the total bandwidth in the \(x\) and \(y\) axes are
\[
\Delta k_x \approx 2k_x^{bw} \approx \frac{4\pi(D_x^2 + D_y^2)}{\lambda \sqrt{2(D_x^2 + D_y^2)^2 + z_0^2}}.
\]
\[
\Delta k_y \approx 2k_y^{bw} \approx \frac{4\pi(D_x^2 + D_y^2)}{\lambda \sqrt{2(D_x^2 + D_y^2)^2 + z_0^2}}. \]
\[(63)\]

where the physical lengths of the SAR aperture and the target distance are depicted in Fig. 1. Hence, the horizontal (\(x\)-axis) and vertical (\(y\)-axis) cross-range resolutions become
\[
\delta_x \approx \frac{2\pi}{\Delta k_x} \approx \frac{\lambda \sqrt{(D_x^2 + D_y^2)^2 + z_0^2}}{2(D_x^2 + D_y^2)^2},
\]
\[
\delta_y \approx \frac{2\pi}{\Delta k_y} \approx \frac{\lambda \sqrt{(D_x^2 + D_y^2)^2 + z_0^2}}{2(D_x^2 + D_y^2)^2}. \]
\[(64)\]

For an aperture-limited system with range \(z_0\) much greater than the aperture size \(D_x^2\) and \(D_y^2\), the cross-range resolutions can be approximated for the center of the imaging scene (i.e. \(D_y^2 = D_x^2 = 0\) as [4], [5]
\[
\delta_x \approx \frac{\lambda z_0}{2D_x^2}, \quad \delta_y \approx \frac{\lambda z_0}{2D_y^2}. \]
\[(65)\]

VI. IMAGING HARDWARE PROTOTYPE

A. SYSTEM OVERVIEW

A mmWave imaging prototype system has been built using commercial off-the-shelf (COTS) components to validate
the proposed image reconstruction techniques and theoretical relationships established between image and wavenumber domains. The prototype system consists of a mmWave radar, a two-axis mechanical scanner, a motor controller, and a host personal computer (PC). The mmWave radar is combination of three hardware modules from Texas Instruments: (1) IWR1443-Boost, (2) mmWave-Devpack, and (3) TSW1400 boards as shown in Fig. 7a.

IWR1443-Boost is an evaluation module based on the single-chip IWR1443 mmWave sensor. It features FMCW transceiver with a 4 GHz frequency bandwidth from 77 GHz to 81 GHz. It integrates four receive and three transmit antennas making an ideal candidate for sparse MIMO array configurations. Fig 8a shows the physical antenna layout of IWR1443-Boost and its corresponding virtual array configuration. In the default layout, the receive antennas are uniformly spaced along y-axis by λ/2 (tuned to the center frequency of 79 GHz). Transmit antennas are also uniformly spaced in y-axis by λ with the exception of the second transmitter, which has an offset of λ/2 along x-axis. In the imaging experiments, we select different antenna pairs (i.e., virtual channels) to emulate various sparse MIMO operations.

TSW1400 and mmWave-Devpack are add-on boards used with IWR1443-Boost to enable high speed raw data capture for post processing. Captured raw data are imported to the host PC with a serial port. The positional accuracy of the scanning is about 0.05 mm. While the current scanner is slow, our goal is to demonstrate the proof of concept. We are working on a much faster mechanical scanner, and we will report our results in a future article.

The diagram shown in Fig. 8b is a simplified view of the main elements and the high-level system architecture of the imaging system. Both radar and rail system are controlled via a MATLAB graphical user interface (GUI) shown in Fig. 9.

**B. MIMO ARRAY CALIBRATION**

In a practical system, measurement errors in the MIMO array may arise due to sensor gain and phase mismatches. Especially, phase mismatches can affect the image reconstruction adversely. In fact, the algorithms proposed in this paper are derived under the assumption that the response of the imaging system is known.

In this paper, we utilize a well-known calibration method for multistatic radar systems based on the ideal backscattered signal model from a reference point target (a corner reflector) at a known position. Let us define the total round-trip delay τ_ℓ of the FMCW signal reflected off the point target between the u_th transmit and v_th receive antennas, and the corresponding transceiver gain α_ℓ. We model the delays between antenna pairs as the superposition of a common instrument delay and residual delays between antenna elements: τ_ℓ = τ_i + τ_c. Ignoring the additive noise, the uncalibrated measured beat signal (see Section II-D) can be defined as

\[
\hat{s}_i(t) = a_s e^{i2\pi(f_0 + K t)(\tau_i + \tau_c)} = a_s e^{i\phi_i} e^{i2\pi f_i t} s_i(t),
\]

where s_i(t) is the reference beat signal model, f_i = K \tau_i is the beat frequency that cause a range bias in the system, and η_ℓ is the residual complex gain factor. Given the measurements \(\hat{s}_i(t)\), the calibration error signal can be computed by a simple demodulation process

\[
w_\ell(t) = \hat{s}_\ell(t) \ast \hat{s}_\ell^*(t),
\]

where (\cdot)^* denotes the complex-conjugate operation. Estimating \(\hat{f}_\ell\) and \(\eta_\ell\) from (67) reduces to the parameter estimation problem of a single-frequency complex tone from noisy observations [37], [38]

\[
\hat{f}_\ell = \arg \max_f \sum_{\ell} |W_\ell(f)|^2,
\]

where \(W_\ell(f)\) is defined as

\[
W_\ell(f) = \int_0^T w_\ell(t)e^{-i2\pi f t} dt.
\]

Finally, the complex gain factors \(\eta_\ell\) for each transceiver pair can be computed by plugging the estimate \(\hat{f}_\ell\) in (66).
FIGURE 8. (a) MIMO array topology of IWR1443-Boost with three transmit and four receive antenna elements, and corresponding virtual array. (b) The hardware architecture of mmWave imager prototype.

FIGURE 9. MATLAB GUI for MIMO-SAR imaging. (a) Platform and radar configuration menu tab. (b) SAR scenario generation menu tab.

FIGURE 10. Measured PSF along \(x\)-axis provides the lateral image resolution that can be achieved by the imaging prototype system at a distance of 808 mm.

FIGURE 11. Measured PSF along \(y\)-axis demonstrates the impact of subsampling in spatial domain. Two visible artifacts are due to aliasing within the visible region.

VII. MEASUREMENTS AND IMAGING RESULTS
The reconstruction quality of the imaging systems is described by the point spread function (PSF). We measure the PSF of our system using a corner reflector. Then, simulations are performed to examine the potential of the proposed algorithms. Finally, the experimental image results of uncovered and concealed targets are provided.

In all experiments, FMCW waveforms are configured to vary from \(f_0 = 77.38\) GHz to \(f_T = 80.93\) GHz, where the signal duration \(T \approx 56.02\) \(\mu\)s and the frequency slope \(K \approx 63.37\) MHz/\(\mu\)s. The wavelength \(\lambda\) is computed according to the center frequency of 79 GHz unless otherwise noted. The target distance \(z_0\) is estimated from the index of the maximum of the combined range spectrum computed.
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**FIGURE 12.** Simulated image reconstruction scenario with sparsely sampled aperture data: (a) simulated sparse MIMO array with three transmit and three receive antenna elements, and corresponding virtual array, (b) reconstructed image from single channel (1st), and (c) reconstructed image from nine channels combined using properly chosen \( w \) gains.

**FIGURE 13.** Various experimental images of the small test target: (a) optical, (b) reconstructed from single channel (1st), (c) reconstructed from three channels (1st, 4th, and 12th) combined without any correction factor, and (d) reconstructed from three channels (1st, 4th, and 12th) combined using properly chosen \( w \) gains.

from the beat signals. The image slices obtained at multiple frequencies from \( f_0 = 77.38 \text{ GHz} \) to \( f_T = 80.93 \text{ GHz} \) are coherently combined to form the final image. Before the image reconstruction process, each subchannel is calibrated as detailed in Section VI-B. All the images presented here are reconstructed on a host PC with Intel Core i7-7700 3.6 GHz central processing unit (CPU) and 64 gigabytes of random access memory (RAM).
A. MEASURED POINT SPREAD FUNCTION

To demonstrate the experimental image resolution of our hardware prototype, we measure the PSF along $x$–axis between a transmit and receive antenna pair of MIMO radar. The measured PSF is shown in Fig. 10. In this measurement, a corner reflector is placed at a distance of $z_0 = 808$ mm in front of the scanner. The scanner moves the radar along $x$–axis. The speed of the scan and radar chirp intervals are configured such that a sampling distance of $\Delta x \approx 0.96$ mm ($\approx \lambda/4$) is realized. The SAR aperture length is $D_x = 400$ mm along the scanning direction. As given in (64), the theoretical image resolution under this configuration is about $\delta_x \approx 4$ mm. As shown in Fig. 10, the measured PSF demonstrates the same theoretical image resolution.

An important contribution of this investigation is to establish the analytical relationship between imaging ambiguities and the subsampled SAR aperture parameters. The measured response of a single transceiver pair along $y$–axis generated with a sampling distance of $\Delta y \approx 7.59$ mm (well over the required Nyquist interval) shows the presence of two imaging artifacts (i.e., ghosts), as shown in Fig. 11. In this experiment, the same corner reflector is placed at a distance of $z_0 = 808$ mm in front of the imager. The radar is configured with the same chirp parameters. We verify the positions of two artifacts along the $y$–axis due to subsampling using the expression in (51) as

$$y_{mn}|_{m=0,n=\pm 1} = \pm \frac{k_y^2 z_0}{4 k^2 - (k_y)^2} \approx 213.3 \text{ mm},$$

at the center frequency of $f_0 = 77.38$ GHz, where the ghost image positions marked in Fig. 11 confirm the estimated ones above.

B. SIMULATED IMAGING RESULTS

To evaluate the performance of the proposed algorithm for recovering ghost-free images when both axes are subsampled, a simulation scenario is performed. A 50 mm by 75 mm small test target, which has different types of small cutouts, is simulated and placed at a distance of $z_0 = 282$ mm from the scanner. The size of the SAR aperture is $D_x \approx 200$ mm by $D_y \approx 200$ mm. The spatial sampling intervals are selected as $\Delta x = \Delta y = 8$ mm. An arbitrary sparse MIMO array with three transmit and three receive antennas shown in Fig. 12a is simulated.
SAR aperture is subsampled along both $x$ and $y$ axes. The reconstructed image shown in Fig. 12b using a single virtual channel shows eight ghosts targets within the visible region of $200 \text{ mm} \times 200 \text{ mm}$ as expected. The ghosts are located at a distance of $(0, \pm 68.8 \text{ mm})$, $(\pm 68.8 \text{ mm}, 0)$, and $(\pm 71.0 \text{ mm}, \pm 71.0 \text{ mm})$ from the correct target as predicted in (51). Fig. 12c shows the alias-free image obtained using nine sparse channels with properly chosen $w$ gains such that the all eight ghosts are canceled. On the other hand, an ideal imaging system, which needs $\lambda/4 \approx 0.95 \text{ mm}$ spacing between the measurement points, would employ a uniform 2-D array with about 80 virtual elements.

C. EXPERIMENTAL IMAGING RESULTS

The imaging process and the proposed image reconstruction algorithms with subsampled SAR aperture are experimentally verified with screening various targets. The antenna layout of IWR1443-Boost in Fig. 8a enables to emulate sparse MIMO configurations along $y-$axis. Therefore, in all experiments, we configure the MIMO-SAR setup in Fig. 1 to create various sparsely sampled aperture scenarios along $y-$axis. As discussed in Section II-B, TDM technique is employed across the transmitters of IWR1443-Boost module. Table 1 summarizes the common system parameters used in each experiment.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Fig. 13</th>
<th>Fig. 14</th>
<th>Fig. 15</th>
<th>Fig. 16</th>
<th>Fig. 17</th>
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</thead>
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<td>$B$ (GHz)</td>
<td>3.55</td>
<td>3.55</td>
<td>3.55</td>
<td>3.55</td>
<td>3.55</td>
</tr>
<tr>
<td>$K$ (MHz/μs)</td>
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<td>63.37</td>
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<tr>
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<td>56.02</td>
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<tr>
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<td>200</td>
<td>400</td>
<td>400</td>
</tr>
<tr>
<td>$D_y$ (mm)</td>
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<td>400</td>
<td>200</td>
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<td>400</td>
</tr>
<tr>
<td>$z_0$ (mm)</td>
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<td>288</td>
<td>270</td>
<td>254</td>
</tr>
<tr>
<td>$\Delta_x$ (mm)</td>
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<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
</tr>
<tr>
<td>$\Delta_y$ (mm)</td>
<td>8</td>
<td>7.59</td>
<td>8</td>
<td>7.59</td>
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</tr>
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</table>

A small test target with a size of $50 \text{ mm}$ by $75 \text{ mm}$ is cut out from a copper clad laminate to create a similar imaging setup to simulations. The test target has similar small cutouts as shown in Fig. 13a. In this scenario, the target is placed at a distance of $z_0 = 280 \text{ mm}$ from the scanner. The SAR aperture is synthesized to cover an area of $D^S_x \approx 200 \text{ mm}$.
by $D_y^x \approx 200$ mm. This configuration provides the lateral resolution of $\delta_x = \delta_y \approx 3$ mm. The spatial sampling intervals are selected as $\Delta_x \approx 0.98$ mm and $\Delta_y = 8$ mm along $x$ and $y$ axes, respectively. The measurement time required to scan the entire aperture, which is limited by the relatively slow linear rails as discussed in Section VI-A, is about 4 min.

The sampling interval along $x$–axis satisfies the Nyquist criterion. On the other hand, SAR aperture along $y$–axis is subsampled. The reconstructed image shown in Fig. 13b using a single virtual channel shows two obvious ghosts (false copies) along $y$–axis within the visible region of 200 mm $\times$ 200 mm. The correct target suffered from aliasing is at the center of the image. The ghosts are located at a distance of $\pm 68.4$ mm for $m = 0$ and $n = \pm 1$ from the correct target as predicted by theoretical results. Fig. 13c shows the image reconstructed by coherently combining the signals from the 1st, 4th, and 12th virtual channels without any correction factor. The ghosts due to aliasing are partially removed but not completely. In Fig. 13d, the reconstruction method presented in Section IV-D is applied and the spectrum from the same subchannels are coherently combined with the properly chosen weights $w$ from (59) to eliminate all ghosts. This demonstrates that the image can be reconstructed without aliasing in a subsampled scenario ($\Delta_y = 8$ mm $> 2\lambda$) using a sparse virtual array. The reconstruction of the image slices at each frequency takes less than 100 ms. Hence, the processing time of the final image formation using 64 uniformly spaced frequencies is about 6 s. The latency introduced by MATLAB would be considered in real-time practical implementations.

In the second imaging experiment, a bigger test target with dimensions 100 mm by 150 mm (shown in Fig. 14a) is cut to illustrate the distortion due to aliasing more effectively. The target distance is $z_0 = 275$ mm and the SAR aperture size is about 400 mm $\times$ 400 mm. Under this configuration, the lateral resolution is approximately 1.6 mm. The spatial sampling intervals are selected as $\Delta_x \approx 0.98$ mm and $\Delta_y = 7.59$ mm.

The sampling interval along $x$–axis satisfies the Nyquist criterion. However, the aperture is subsampled along $y$–axis. Fig. 14b shows the reconstructed image from a single channel. The image has four ghosts within a visible region of 400 mm $\times$ 400 mm. The ghosts are located at a distance of $\pm 71.0$ mm and $\pm 158.8$ mm for $m = 0$, $n = \pm 1$, and $n = \pm 2$ from the correct target, as predicted by theoretical expressions. Fig. 14c shows the image obtained by combining signals from the 1st, 7th, and 11th channels with properly chosen $w$ gains such that the first two ghosts are canceled. Fig. 14d shows the ghost-free image obtained using the 1st, 2nd, 6th, 7th, and 11th channels.

The third imaging experiment demonstrates the capability of the prototyped system for screening of concealed items. The smaller test target in Fig. 13a is concealed in a cardboard box as shown in Fig. 15a. The box is placed at a distance of $z_0 = 288$ mm from the scanner. The SAR aperture size and the spatial sampling intervals are same as the first imaging experiment. Therefore, the imaging scenario is subsampled along $y$–axis. The reconstructed image of a single channel shown in Fig. 15b shows four ghost targets within a visible region of 400 mm $\times$ 400 mm. The ghosts are located at a distance of $\pm 70.3$ mm and $\pm 155.2$ mm from the correct target, where the experimental locations satisfy the exact theoretical result. In Fig. 15c, the images from the 2nd, 4th, and 10th channels are coherently combined with properly chosen $w$ gains to cancel the first two ghost targets. Fig. 15d shows the image obtained by combining the spectrum of the 1st, 3rd, 9th, 10th, and 12th channels with properly chosen $w$ gains such that all four ghosts are canceled.

Finally, two additional experiments are performed to demonstrate the capability of the prototyped system in real-world security screening scenarios. In both experiments, the SAR aperture size is about 400 mm $\times$ 400 mm. The spatial sampling intervals are selected as $\Delta_x \approx 0.98$ mm and $\Delta_y = 7.59$ mm. The eight virtual channels (1st to 4th and 9th to 12th) are used with their properly chosen $w$ complex gains. For both scenarios, the lateral resolution achieved is about 1.6 mm.
and a pair of tweezers) concealed in a cardboard box. Fig. 16b shows the reconstructed image focused at \( z_0 = 270 \) mm. All the objects are clearly visible without spatial aliasing.

Fig. 17a shows the final imaging scenario for a security screening application. Smaller objects (a pair of small scissors, two coins, a knife, a nail clipper, a pair of small tweezers, a key, and a leather wallet) are concealed in a leather bag. Fig. 17b shows the reconstructed image focused at \( z_0 = 254 \) mm. All the objects are clearly identified, even the non-metallic wallet and very small objects such as key and nail cutter.

**FIGURE 17.** Imaging scenario with small items concealed in a leather bag: (a) optical image, and (b) reconstructed image from eight channels combined using properly chosen w gains.

**VIII. CONCLUSION**

In this paper, we presented a near-field mmWave imaging system utilizing 2-D MIMO array in SAR configuration. We proposed and experimentally verified a computationally efficient novel image reconstruction algorithm based on sparsely sampled aperture data. We analyzed the effect of sparse sampling both on wavenumber spectrum and spatial domains. We involved the calibration method for MIMO array, as well as the complete signal processing chain necessary for the image formation. We investigated the design considerations including the system’s bandwidth, spatial sampling criteria, and image resolution. We built a mmWave imaging prototype using commercially available MIMO sensors to validate the proposed image reconstruction method with measurements. We characterized the system performance by the evaluation of PSF, simulations, and real images. The results show that the prototyped system is able to achieve high image quality with a significantly reduced number of antenna elements, thus making the system more affordable and less complex.

**APPENDIX A**

**FOURIER TRANSFORM DEFINITIONS**

The 2-D spatial Fourier transform and its inverse are defined by

\[
S(k_x, k_y) = \iint s(x, y) e^{-j(k_x x + k_y y)} \, dx \, dy
= \text{FT}_{2D}[s(x, y)],
\]

\[
s(x, y) = \frac{1}{(2\pi)^2} \iint S(k_x, k_y) e^{j(k_x x + k_y y)} \, dk_x \, dk_y
= \text{IFT}_{2D}[S(k_x, k_y)].
\]

If the function is shifted in the spatial domain, there is a corresponding phase shift in the Fourier domain:

\[
\text{FT}_{2D}[s(x - x_0, y - y_0)] = e^{-j(k_x x_0 + k_y y_0)} S(k_x, k_y).
\]

If the function is shifted in the Fourier domain, there is a corresponding phase shift in the spatial domain:

\[
\text{IFT}_{2D}[S(k_x - k_x^0, k_y - k_y^0)] = e^{j(k_x^0 x + k_y^0 y)} s(x, y).
\]

The 2-D spatial Fourier transform of a 2-D spatial impulse train is given by

\[
\text{FT}_{2D}\left[ \sum_{p \in \mathbb{Z}} \sum_{q \in \mathbb{Z}} \delta(x - p\Delta_x, y - q\Delta_y) \right]
= \frac{(2\pi)^2}{\Delta_x \Delta_y} \sum_{m \in \mathbb{Z}} \sum_{n \in \mathbb{Z}} \delta(k_x - mk_x^0, k_y - nk_y^0),
\]

where \( k_x^0 \) and \( k_y^0 \) are defined in (34).

Multiplication in the spatial domain corresponds to a convolution in the Fourier domain:

\[
\text{FT}_{2D}[s_1(x, y) \ast s_2(x, y)] = \frac{1}{(2\pi)^2} S_1(k_x, k_y) \ast S_2(k_x, k_y).
\]

Differentiation in the spatial domain yields

\[
\text{FT}_{2D}\left[ \frac{\partial s(x, y)}{\partial x} \right] = jk_x S(k_x, k_y),
\]

\[
\text{FT}_{2D}\left[ \frac{\partial s(x, y)}{\partial y} \right] = jk_y S(k_x, k_y).
\]
APPENDIX B

THE METHOD OF STATIONARY PHASE

The method of stationary phase (MSP) provides an analytical solution for integrands, which have a wide phase variation and an envelope of $g(x, y)$, as [39], [40]

$$
\int \int g(x, y)e^{i\phi(x, y)} \, dx \, dy \approx \frac{j2\pi}{\sqrt{\phi_{xx} \phi_{yy} - \phi_{xy}^2}} \times g(x_0, y_0)e^{i\phi(x_0, y_0)},
$$

(77)

where $\phi(x, y)$ is the phase of the exponential that is assumed to be twice-continuously differentiable. A small neighborhood near the points, where the two first derivatives of $\phi(x, y)$ vanish, gives the major contribution to the integral in (77). These points are known as points of stationary phase, where the phase $\phi(x, y)$ takes an extreme value as

$$
\frac{\partial \phi(x, y)}{\partial x} \bigg|_{(x=x_0, y=y_0)} = 0,
$$

$$
\frac{\partial \phi(x, y)}{\partial y} \bigg|_{(x=x_0, y=y_0)} = 0.
$$

(78)

In (77), $\phi_{xx}$, $\phi_{yy}$, and $\phi_{xy}$ denote the second partial derivatives of $\phi(x, y)$ evaluated at the stationary points. It is assumed that $\phi_{xx}\phi_{yy} - \phi_{xy}^2 \neq 0$. The derivation of (77) is already given in previous studies for single variable [41] or without the envelope $g(x, y)$ factor [21]. Here, the exact analytical solution is given to evaluate the 2-D Fourier transform of spherical wave formula in (19) asymptotically by using MSP.

Substituting (8) into (19), the spherical wave formula becomes

$$
e^{2ikR} \frac{R}{\sqrt{(x - x')^2 + (y - y')^2 + z_0^2}}.
$$

(79)

Using the Fourier transform definitions in Appendix A, the 2-D Fourier transform of (79) is evaluated as

$$
\text{FT}_{2D} \left[ e^{2ikR} \frac{R}{\sqrt{x^2 + y^2 + z_0^2}} \right] = e^{-j(k_x x' + k_y y')} \times \int \int e^{j2k' \sqrt{x^2 + y^2 + z_0^2}} \times e^{-j(k_x x' + k_y y')} \, dx \, dy.
$$

(80)

The double integral above can be solved analytically using MSP in (77). Let us define the phase and the envelope terms in (80) as

$$
\phi(x, y) = 2k\sqrt{x^2 + y^2 + z_0^2} - k_xx - k_yy,
$$

$$
g(x, y) = 1/\sqrt{x^2 + y^2 + z_0^2}.
$$

(81)

(82)

The first derivatives of (81)

$$
\phi_x(x, y) = \frac{\partial \phi(x, y)}{\partial x} = \frac{2kx}{\sqrt{x^2 + y^2 + z_0^2}} - k_x,
$$

$$
\phi_y(x, y) = \frac{\partial \phi(x, y)}{\partial y} = \frac{2ky}{\sqrt{x^2 + y^2 + z_0^2}} - k_y.
$$

(83)

give the stationary points in (78) as

$$
x_0 = \frac{k_x z_0}{\sqrt{4k^2 - k_x^2 - k_y^2}},
$$

$$
y_0 = \frac{k_y z_0}{\sqrt{4k^2 - k_x^2 - k_y^2}}.
$$

(84)

In order to ensure the asymptotic expansion provided by the MSP valid, the coordinates must be both real such that the frequency wavenumber must satisfy the following inequality

$$
k_x^2 + k_y^2 \leq 4k^2.
$$

(85)

Substituting (84) into (81) and (82), the phase and the envelope evaluated at the stationary points yield

$$
\phi(x_0, y_0) = \frac{\sqrt{4k^2 - k_x^2 - k_y^2}z_0}{\sqrt{4k^2 - k_x^2 - k_y^2}},
$$

$$
g(x_0, y_0) = \frac{2kz_0}{\sqrt{4k^2 - k_x^2 - k_y^2}},
$$

(86)

(87)

respectively. Similarly, the second partial derivatives of the phase evaluated at the stationary points are calculated as

$$
\phi_{xx} = \frac{\sqrt{4k^2 - k_x^2 - k_y^2}(4k^2 - k_x^2)}{4k^2z_0},
$$

$$
\phi_{yy} = \frac{\sqrt{4k^2 - k_x^2 - k_y^2}(4k^2 - k_y^2)}{4k^2z_0},
$$

$$
\phi_{xy} = -\frac{\sqrt{4k^2 - k_x^2 - k_y^2}k_xk_y}{4k^2z_0},
$$

(88)

which yields the denominator in (77) as

$$
\sqrt{\phi_{xx}\phi_{yy} - \phi_{xy}^2} = \frac{(4k^2 - k_x^2 - k_y^2)}{2kz_0}.
$$

(89)

Substituting (86), (87) and (89) into (77), the resulting 2-D Fourier transform expression in (80) is expressed as

$$
\text{FT}_{2D} \left[ e^{2ikR} \frac{R}{\sqrt{x^2 + y^2 + z_0^2}} \right] = \frac{j2\pi}{k_\xi} e^{-j(k_\xi x' + k_y y')} \times \int \int e^{j2k_\xi (x - x') + k_y (y - y') + z_0} \, dk_\xi \, dk_y.
$$

(90)

APPENDIX C

MULTIVARIATE TAYLOR SERIES EXPANSION

Let $f$ be an infinitely differentiable real or complex-valued function in some open neighborhood around $x = (x_0, y_0)$. Let $x = [x, y]$ and let $x_0 = [x_0, y_0]$. With this vector notation, the Taylor series of $f(x)$ in a neighborhood of $x_0$ is

$$
f(x) = f(x_0) + [(x - x_0) \cdot \nabla f(x_0)]
$$

$$
+ \frac{1}{2!}[(x - x_0) \cdot H(x_0) \cdot (x - x_0)^T] + \ldots,
$$

(92)
where $\nabla f$ is the vector of first derivatives
\begin{equation}
\nabla f(x, y) = \begin{bmatrix} f_x(x, y) \\ f_y(x, y) \end{bmatrix},
\end{equation}
and $H$ is the matrix of second derivatives, called the Hessian matrix
\begin{equation}
H(x, y) = \begin{bmatrix} f_{xx}(x, y) & f_{xy}(x, y) \\ f_{yx}(x, y) & f_{yy}(x, y) \end{bmatrix}.
\end{equation}

### A. TAYLOR SERIES EXPANSION OF THE ROUND-TRIP DISTANCE

Substituting the transmitter and receiver locations in (6) into (5), the total round-trip distance associated with the $n$th transmitter element at $(x_n, y_n, 0)$ and the $v$th receiver element at $(x_v, y_v, 0)$ to a point scatterer at $(x', y', z_0)$ becomes
\begin{equation}
R_t = \sqrt{(x + d_t^x/2 - x')^2 + (y + d_t^y/2 - y')^2 + z_0^2} + \sqrt{(x - d_t^x/2 - x')^2 + (y - d_t^y/2 - y')^2 + z_0^2}.
\end{equation}

Evaluating the first derivatives of (95) at $(d_t^x = 0, d_t^y = 0)$ yields
\begin{equation}
\frac{\partial R_t}{\partial d_t^x} \bigg|_{(d_t^x=0,d_t^y=0)} = \frac{\partial R_t}{\partial d_t^y} \bigg|_{(d_t^x=0,d_t^y=0)} = 0.
\end{equation}

Similarly, the second partial derivatives of (95) evaluated at $(d_t^x = 0, d_t^y = 0)$ yields
\begin{equation}
\frac{\partial^2 R_t}{\partial (d_t^x)^2} \bigg|_{(d_t^x=0,d_t^y=0)} = \frac{1}{2} \frac{1}{(1 - \frac{(x-x')^2}{R^2})}, \quad \frac{\partial^2 R_t}{\partial (d_t^y)^2} \bigg|_{(d_t^x=0,d_t^y=0)} = \frac{1}{2} \frac{1}{(1 - \frac{(y-y')^2}{R^2})}, \quad \frac{\partial^2 R_t}{\partial d_t^x \partial d_t^y} \bigg|_{(d_t^x=0,d_t^y=0)} = -\frac{1}{2R} \frac{(x-x')(y-y')}{R^3},
\end{equation}
where $R$ is given in (8). Substituting (96) and (97) into (92), quadratic approximation of $R_t$ is given by
\begin{equation}
R_t \approx 2R + \frac{(d_t^x)^2 + (d_t^y)^2}{4R} - \frac{(x-x')(y-y')}{{2R}^3}.
\end{equation}

### B. TAYLOR SERIES EXPANSION OF THE GHOST IMAGE SPECTRUM COMPONENTS

Evaluating the amplitude factor \(^{(41)}\) at $(k_x = mk_x^s, k_y = nk_y^s)$ gives
\begin{equation}
\vartheta(k_x^s, k_y^s) = \frac{G_{mn}}{2k},
\end{equation}
where $G_{mn}$ is given in (44). Similarly, the first derivatives of (41) evaluated at $(k_x = mk_x^s, k_y = nk_y^s)$ yields
\begin{equation}
\frac{\partial \vartheta(k_x, k_y)}{\partial k_x} \bigg|_{(k_x=mk_x^s,k_y=nk_y^s)} = -\frac{mk_x^s}{2kG_{mn}}.
\end{equation}

Substituting (99) and (100) into (92), linear approximation of $\vartheta(k_x, k_y)$ becomes
\begin{equation}
\vartheta(k_x, k_y) \approx \frac{G_{mn}}{2k} - \frac{mk_x^s}{2kG_{mn}}(k_x - mk_x^s) - \frac{nk_y^s}{2kG_{mn}}(k_y - nk_y^s),
\end{equation}
which can be further simplified as
\begin{equation}
\vartheta(k_x, k_y) \approx \frac{2k}{G_{mn}} - \frac{mk_x^s}{2kG_{mn}}k_x - \frac{nk_y^s}{2kG_{mn}}k_y.
\end{equation}

Evaluating the phase factor in (42) at $(k_x = mk_x^s, k_y = nk_y^s)$ results in
\begin{equation}
\varphi(mk_x^s, nk_y^s) = (2k - G_{mn})z_0.
\end{equation}

Similarly, the first derivatives of (42) evaluated at $(k_x = mk_x^s, k_y = nk_y^s)$ yields
\begin{equation}
\varphi(k_x, k_y) \approx (2k - G_{mn})z_0 + \frac{mk_x^s z_0}{G_{mn}}(k_x - mk_x^s) + \frac{nk_y^s z_0}{G_{mn}}(k_y - nk_y^s),
\end{equation}
which can be further simplified as
\begin{equation}
\varphi(k_x, k_y) \approx 2kz_0 \left(1 - \frac{2k}{G_{mn}}\right) + \frac{mk_x^s z_0}{G_{mn}}k_x + \frac{nk_y^s z_0}{G_{mn}}k_y.
\end{equation}

### REFERENCES


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